

# Using radar layers to infer migration of WAIS Divide

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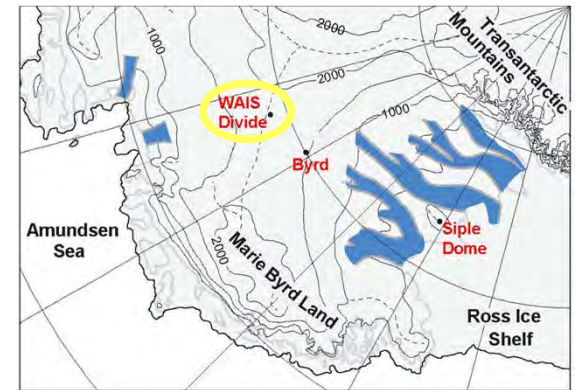
**Howard Conway**      *University of Washington*

**T.J. Fudge**      *University of Washington*

## Background / Motivation

### 1. WAIS Divide ice core drilled to ~3331 m

- Ice at depth is younger than expected – thick layers at depth
- Ice at depth may be colder than expected



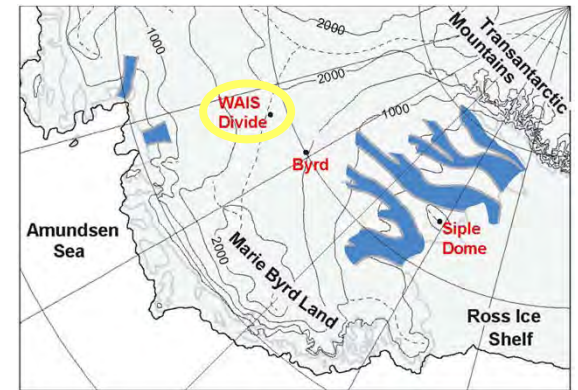
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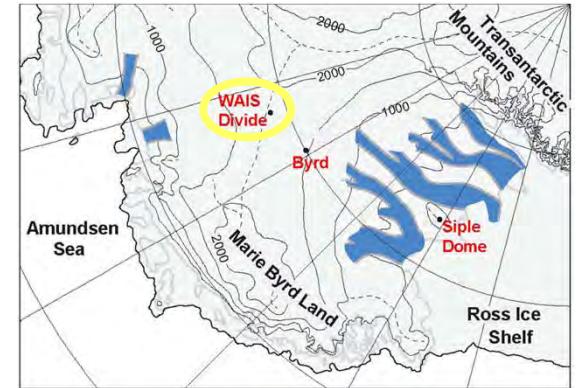
- Ice at depth is younger than expected – thick layers at depth
- Ice at depth may be colder than expected

### 2. WAIS divide is migrating and thinning today (Conway and Rasmussen, 2009)

- Migrating toward Ross Sea at ~10 m/yr and thinning ~8 cm/yr  
*(1000 years at this rate gives 10 km migration and 80 m thinning)*
- Ice-divide position and interior ice thickness likely controlled by ice dynamics



## Background / Motivation



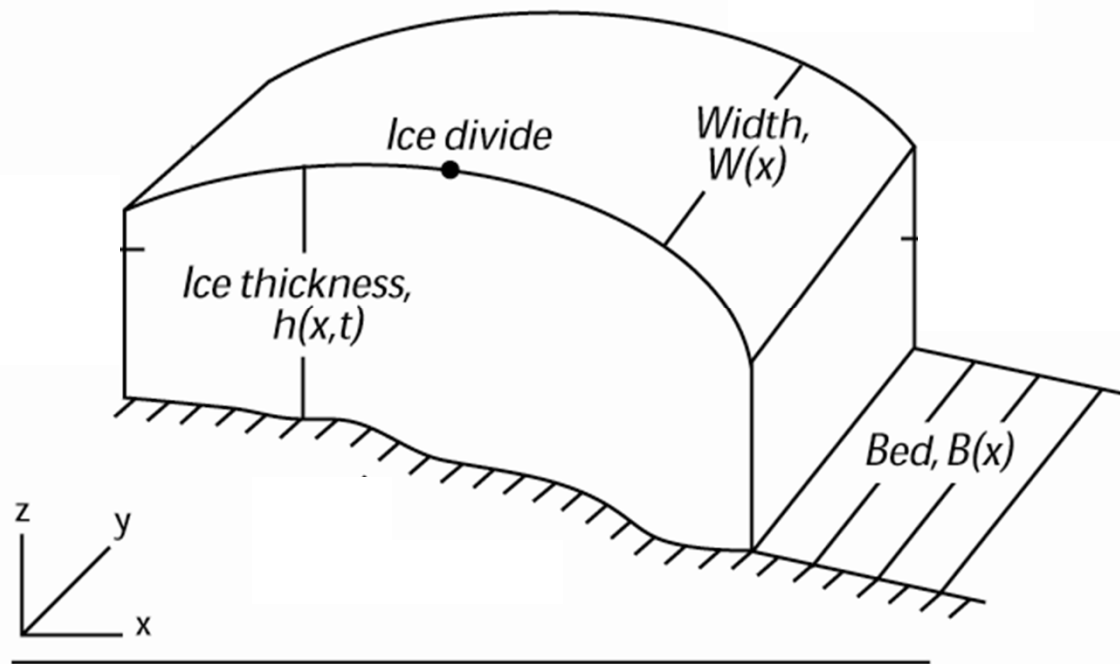
1. WAIS Divide ice core drilled to ~3331 m
  - Ice at depth is younger than expected – thick layers at depth
  - Ice at depth may be colder than expected
2. WAIS divide is migrating and thinning today (Conway and Rasmussen, 2009)
  - Migrating toward Ross Sea at ~10 m/yr and thinning ~8 cm/yr
3. *History* of ice-divide position is unknown
  - Need to inform ice-core interpretation

## Objectives

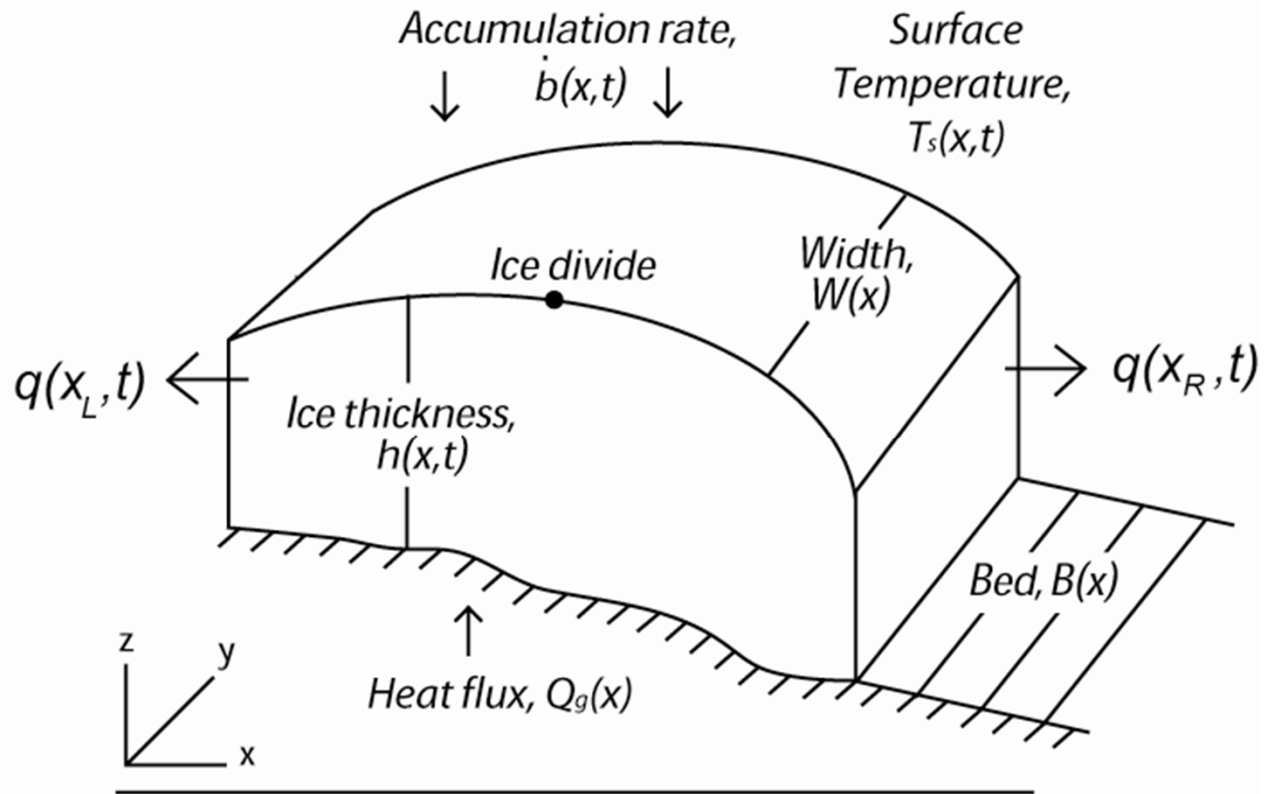
### **1. Compare 2-D ice-sheet model realizations to ice-sheet data:**

- Ice-core depth-age scale
- Ice-temperature profile
- Surface-velocity measurements
- Modern ice-surface profile
- Internal-layer shapes

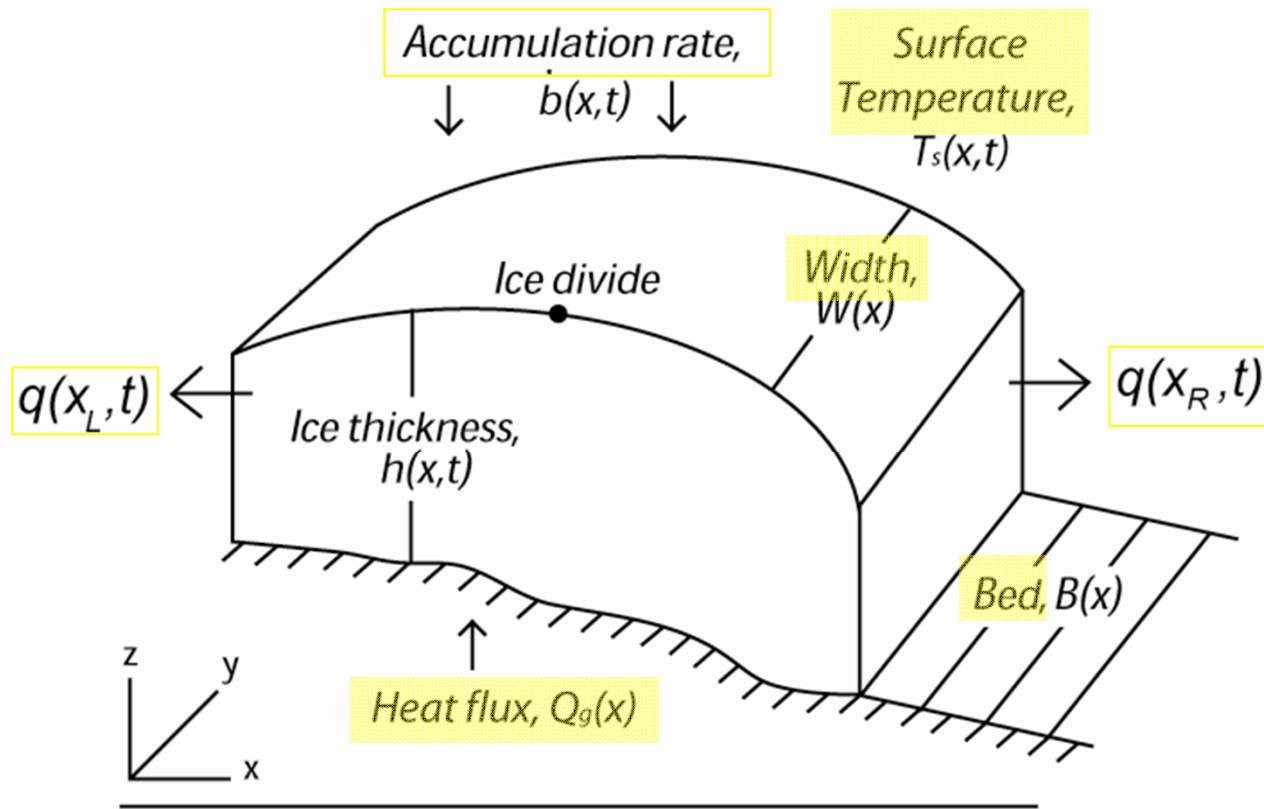
## 2.5-D Ice-sheet flowband model



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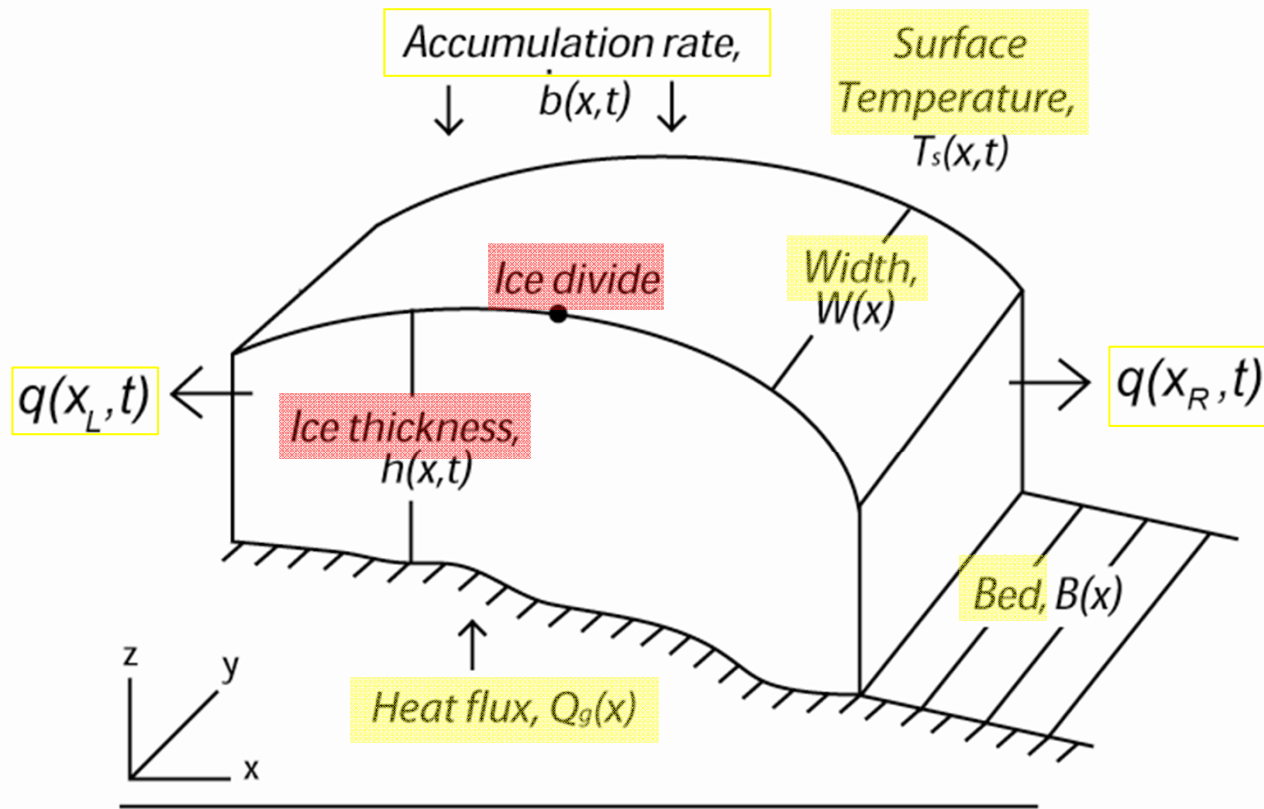
## 2.5-D Ice-sheet flowband model



= Prescribed

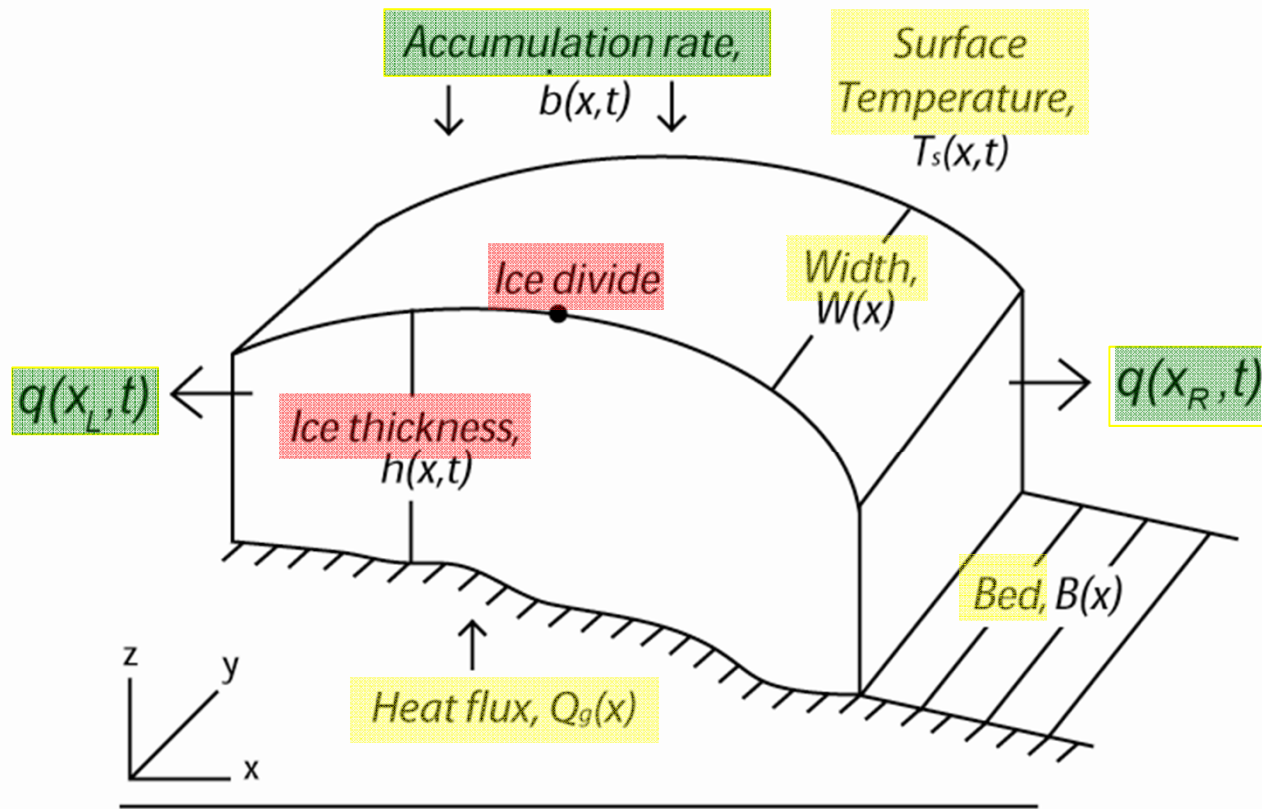


## 2.5-D Ice-sheet flowband model



- = Prescribed
- = Calculated

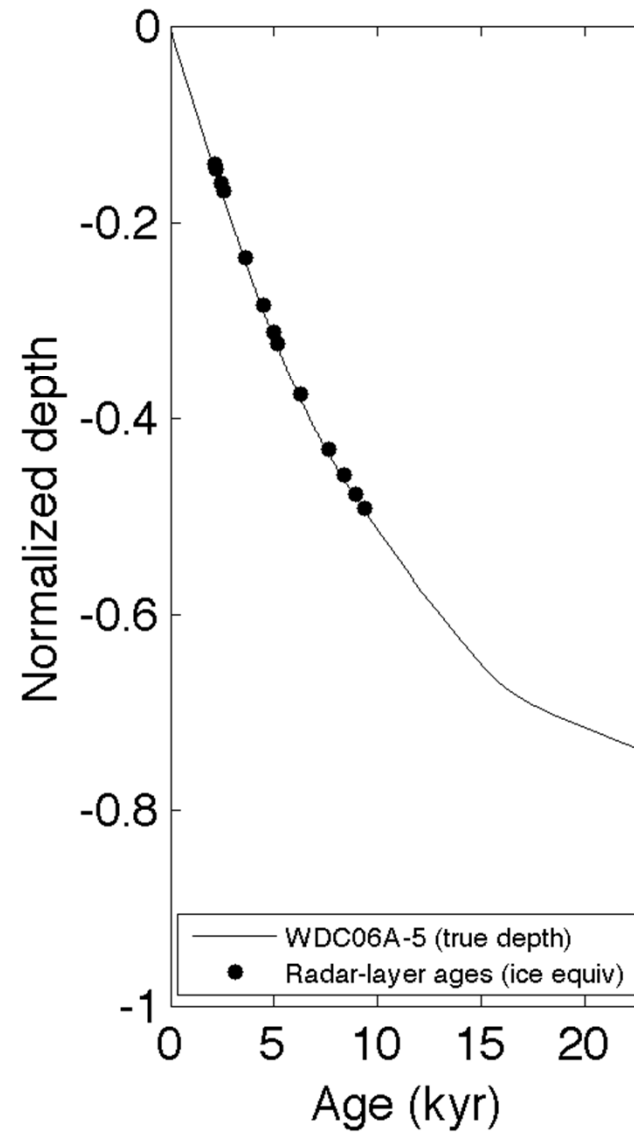
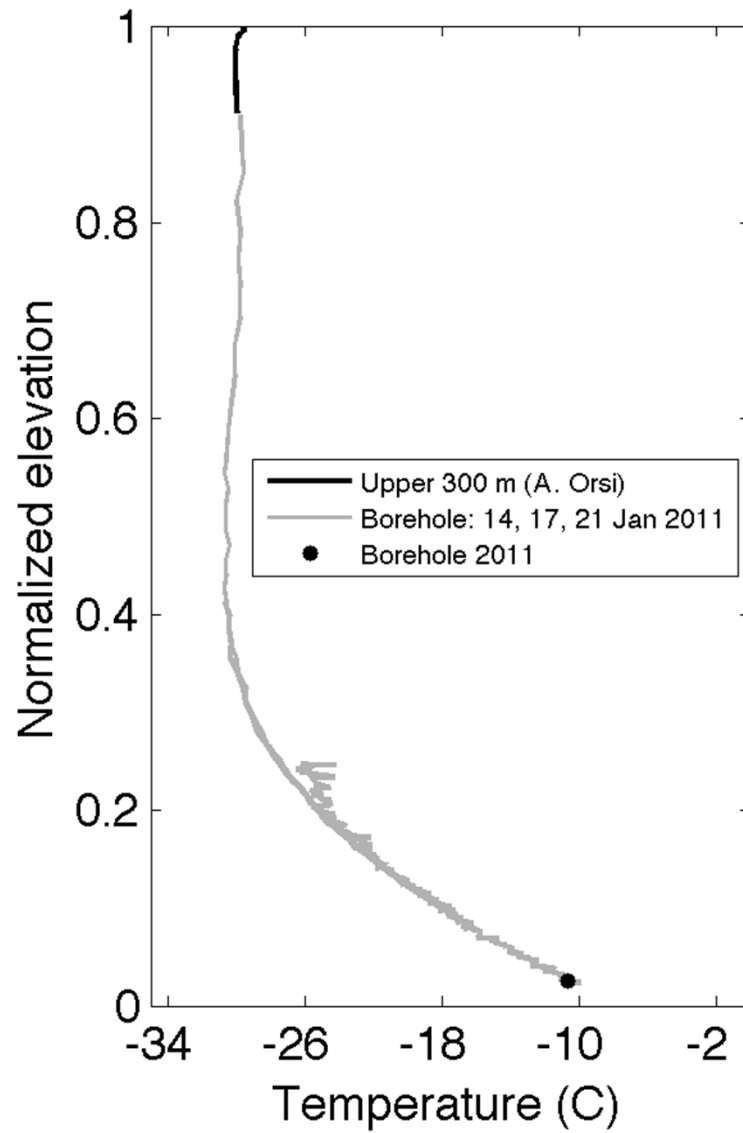
## 2.5-D Ice-sheet flowband model



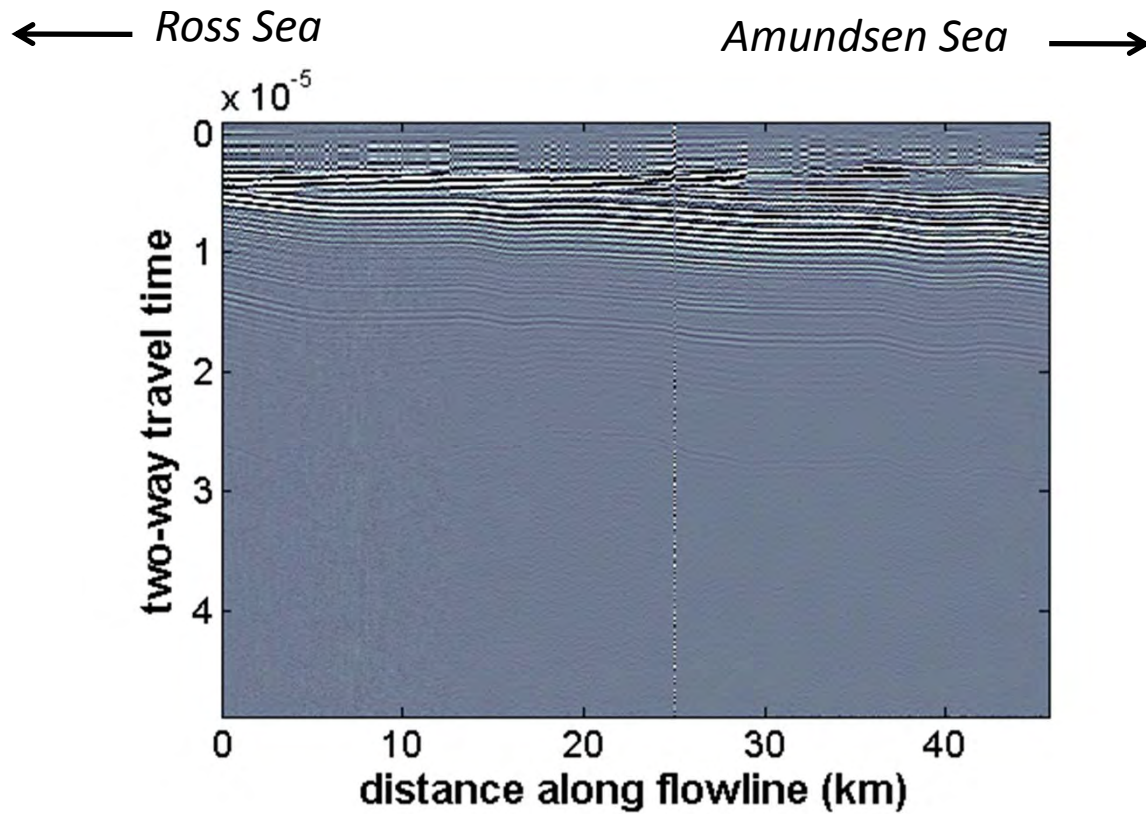
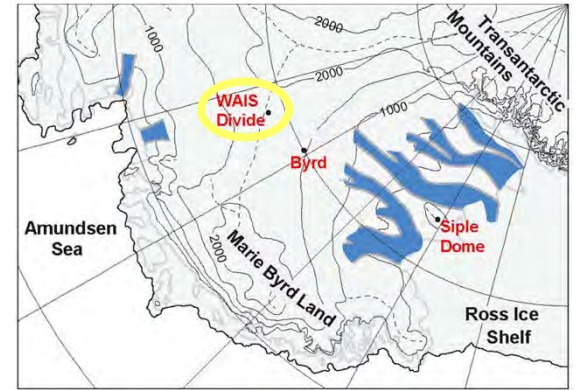
- = Prescribed
- = Calculated
- = Inferred

# Ice temperature and depth-age scale

Data from  
WAIS Divide  
Science Team



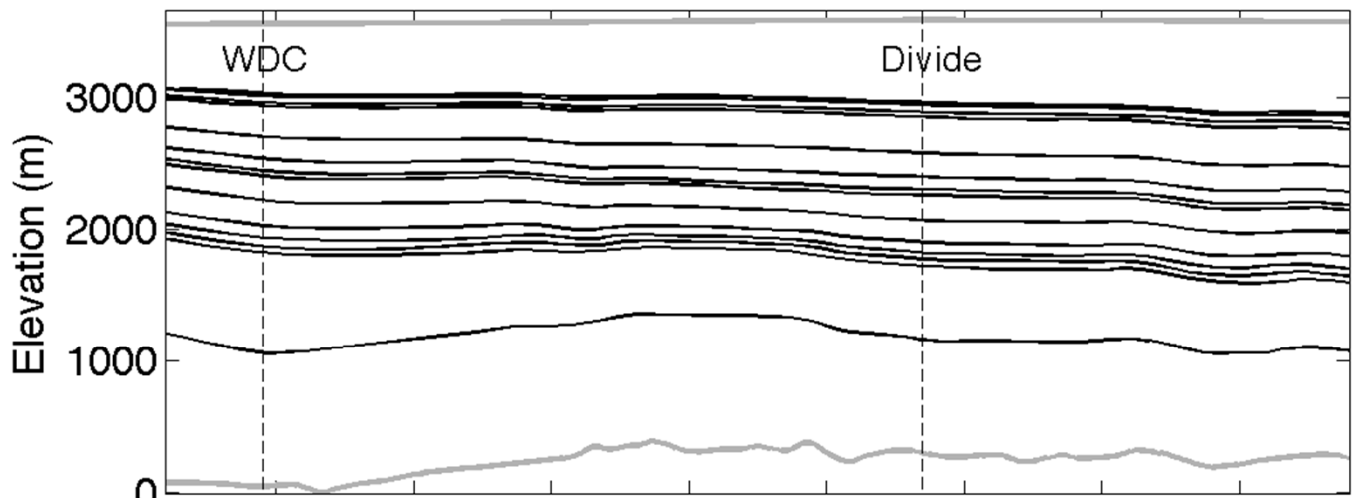
# Internal layers



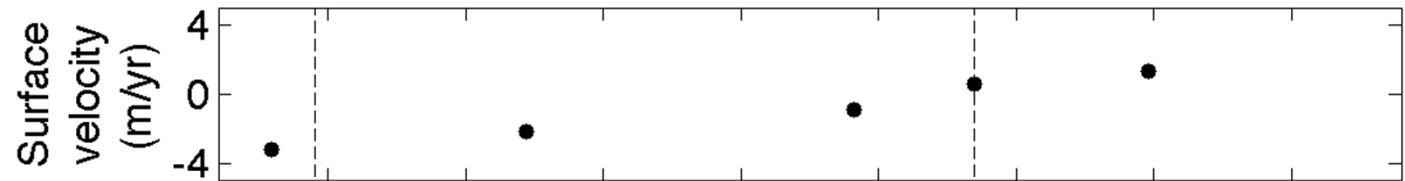
+ ( additional radar data? )

← Ross Sea

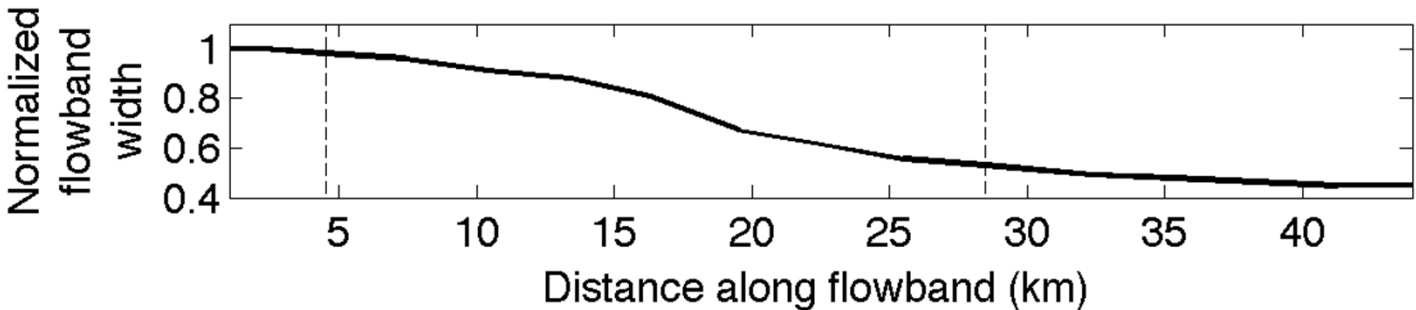
Amundsen Sea →



(e.g. Neumann et al., 2008)



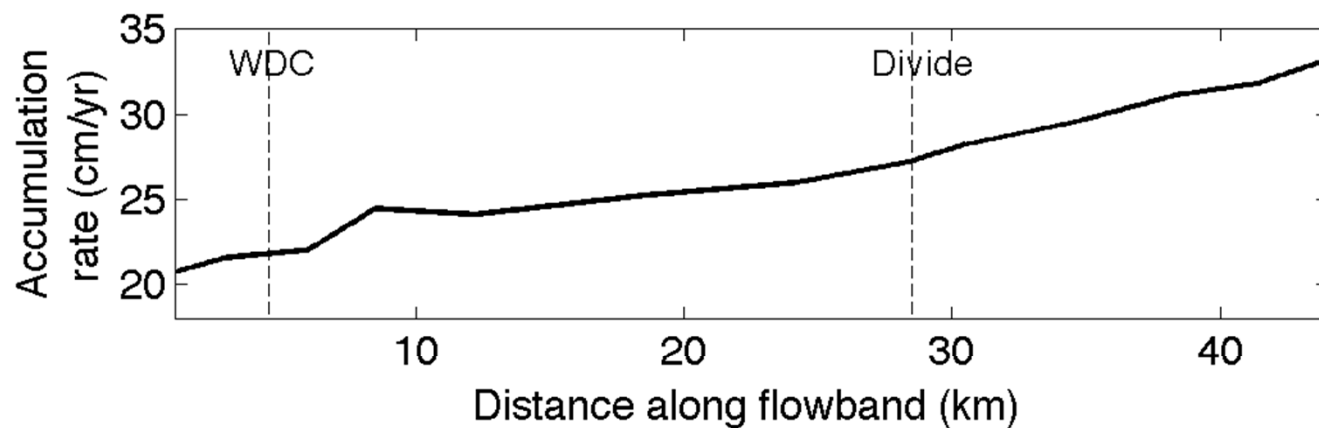
(Conway and Rasmussen, 2009)



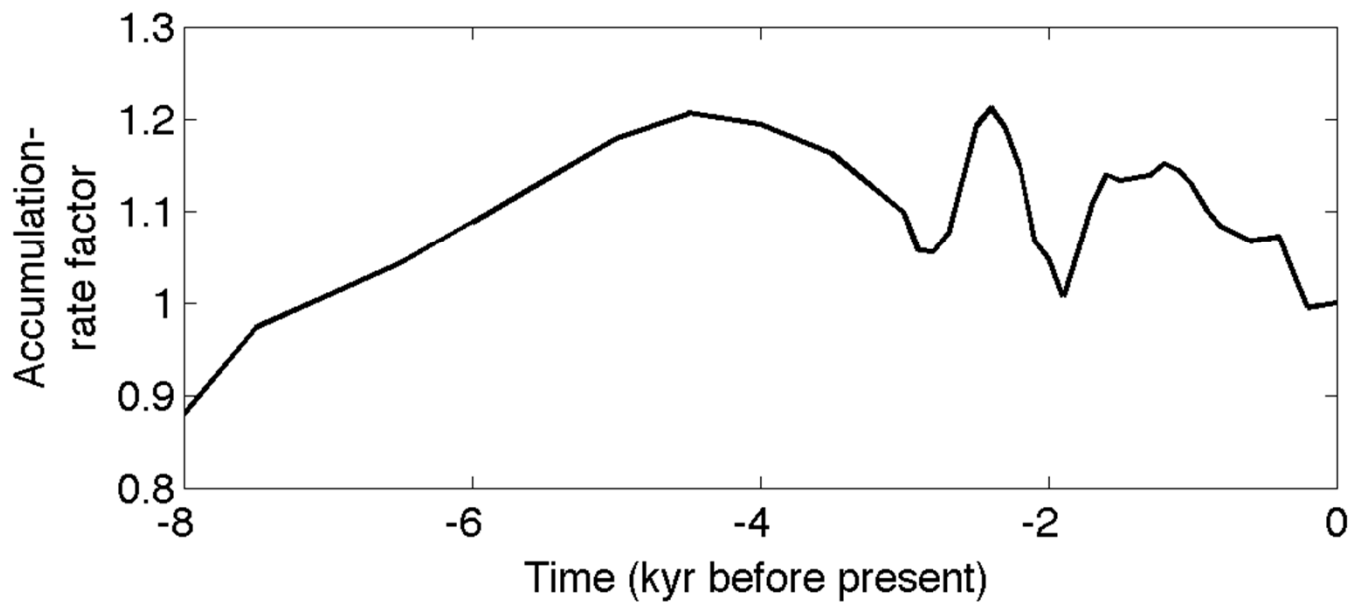
(Neumann and Price, unpublished)

← Ross Sea

Amundsen Sea →



(Neumann et al., 2008)



(Neumann, Price, McConnell, 2010)

# Objectives

## 1. Compare 2-D ice-sheet model realizations to ice-sheet data:

- Ice-core depth-age scale
- Ice-temperature profile
- Surface-velocity measurements
- Modern ice-surface profile
- Internal-layer shapes

**Preliminary** analysis  
in preparation for the  
inverse problem  
incorporating  
new ice-core data

## 2. Solve an inverse problem to infer:

- Accumulation-rate history
- Ice-flow history (external-flux forcing) → ice-divide position

# Objectives

## 1. Compare 2-D ice-sheet model realizations to ice-sheet data:

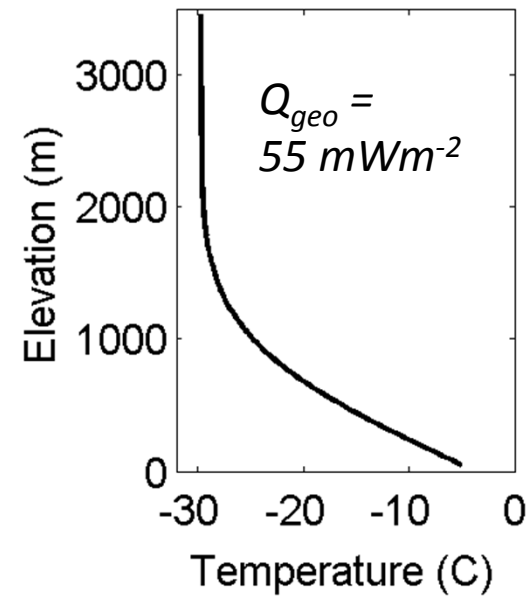
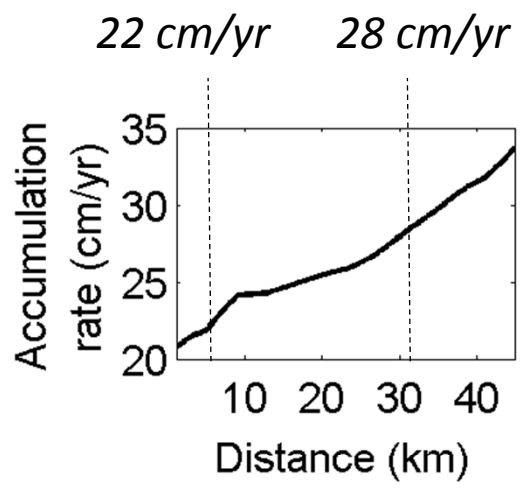
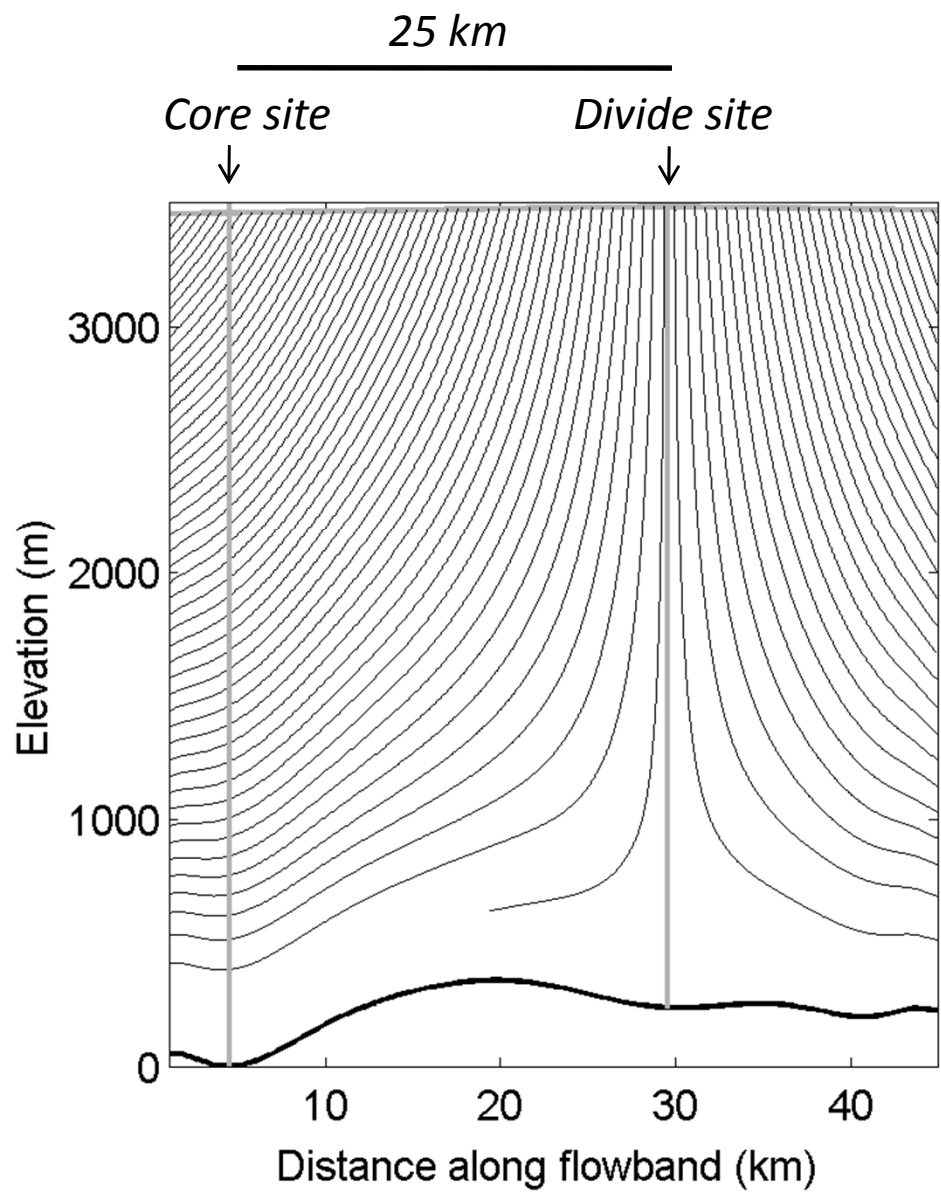
- Ice-core depth-age scale
- Ice-temperature profile
- Surface-velocity measurements
- Modern ice-surface profile
- Internal-layer shapes

How do variations in accumulation rate, temperature, and ice flow affect realizations of the available data?

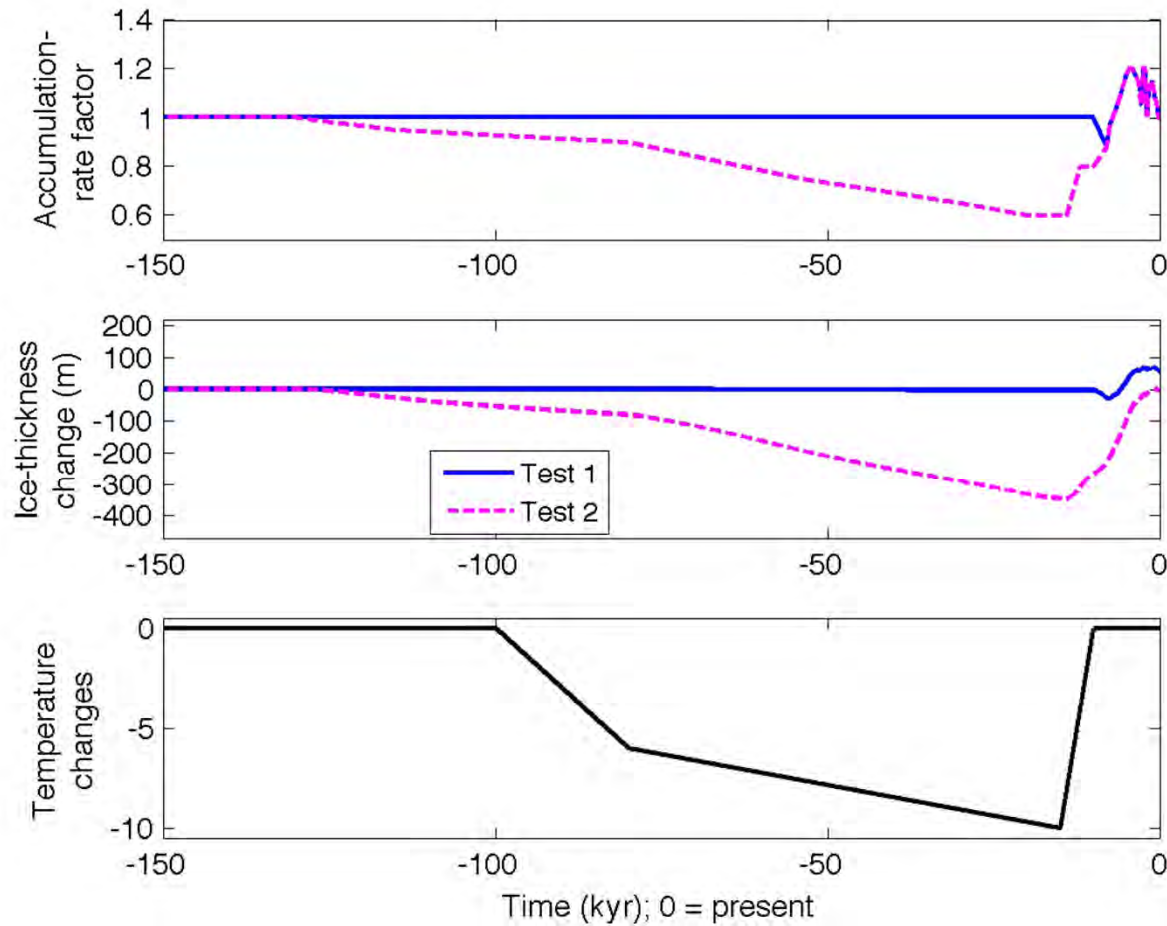
## 2. Solve an inverse problem to infer:

- Accumulation-rate history
- Ice-flow history (external-flux forcing) → ice-divide position



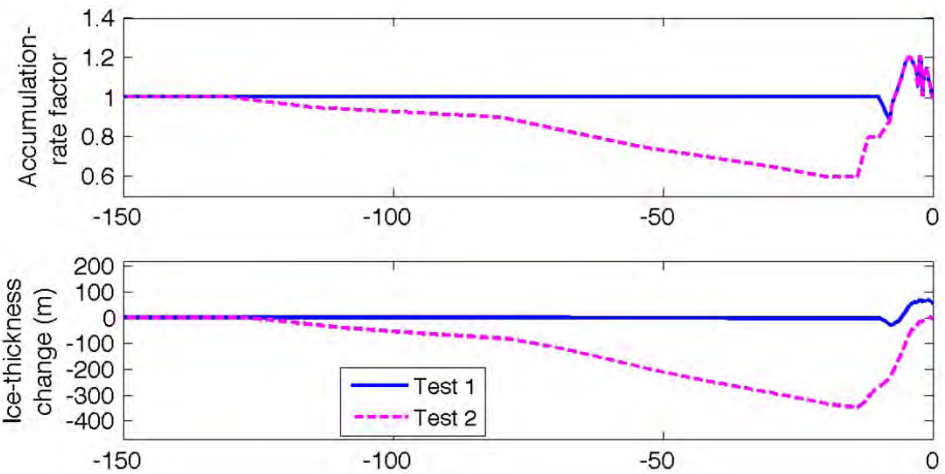
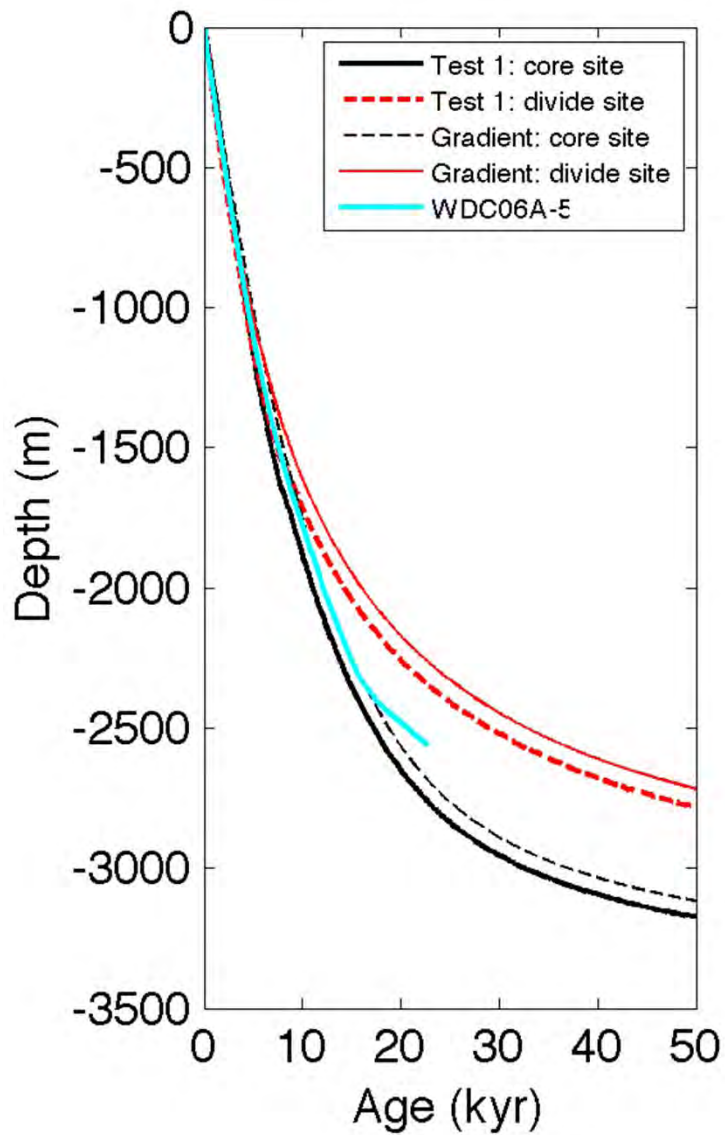


# Changes in accumulation rate



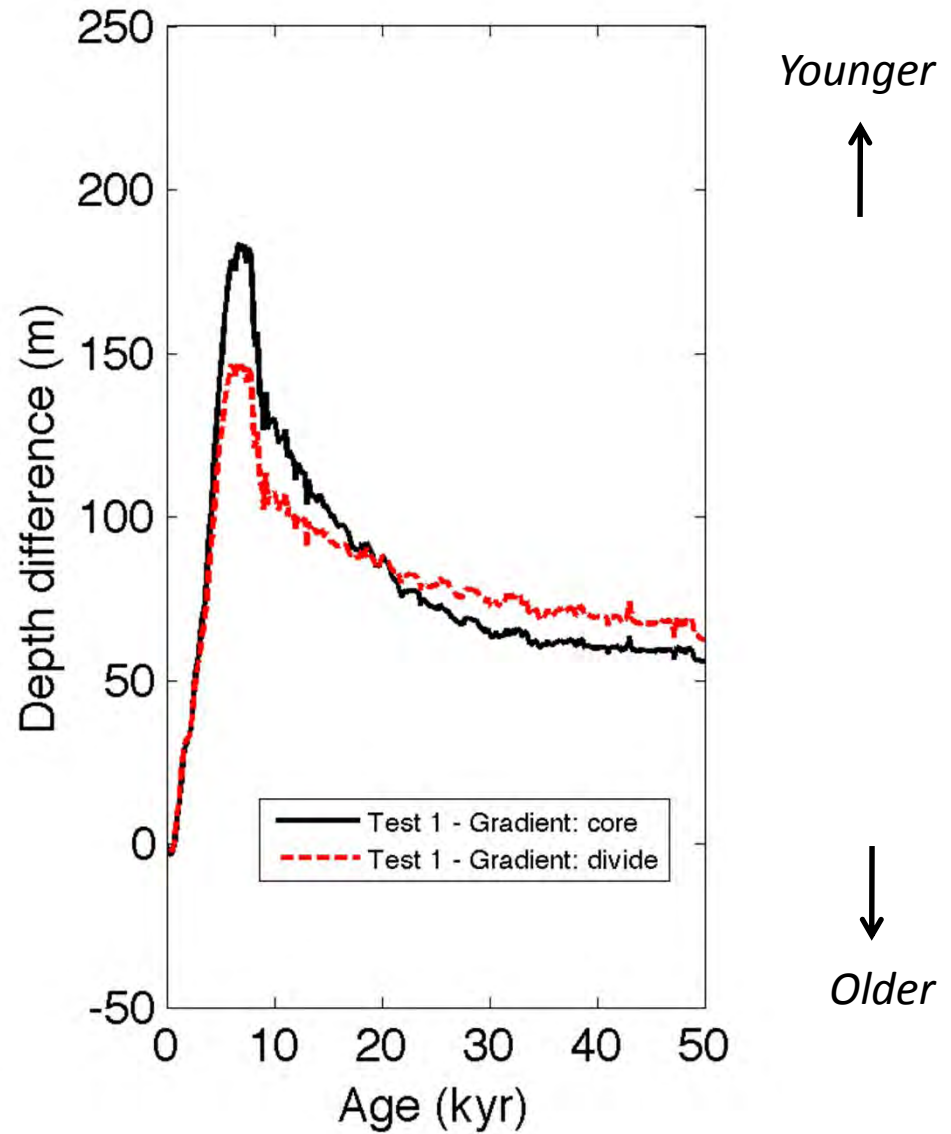
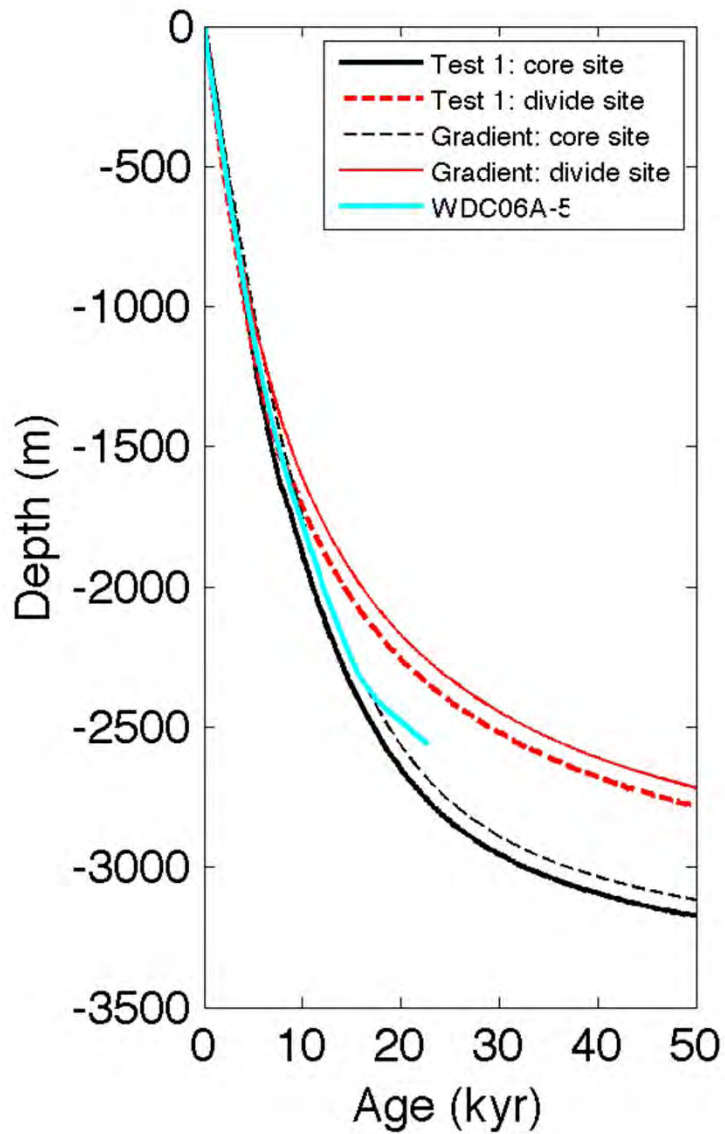
*Test 1:*  
Modern accumulation in the glacial  
Calculated thickness changes  
Surface temperature changes

*Test 2:*  
Decreased accumulation in glacial  
Calculated thickness changes  
Surface temperature changes

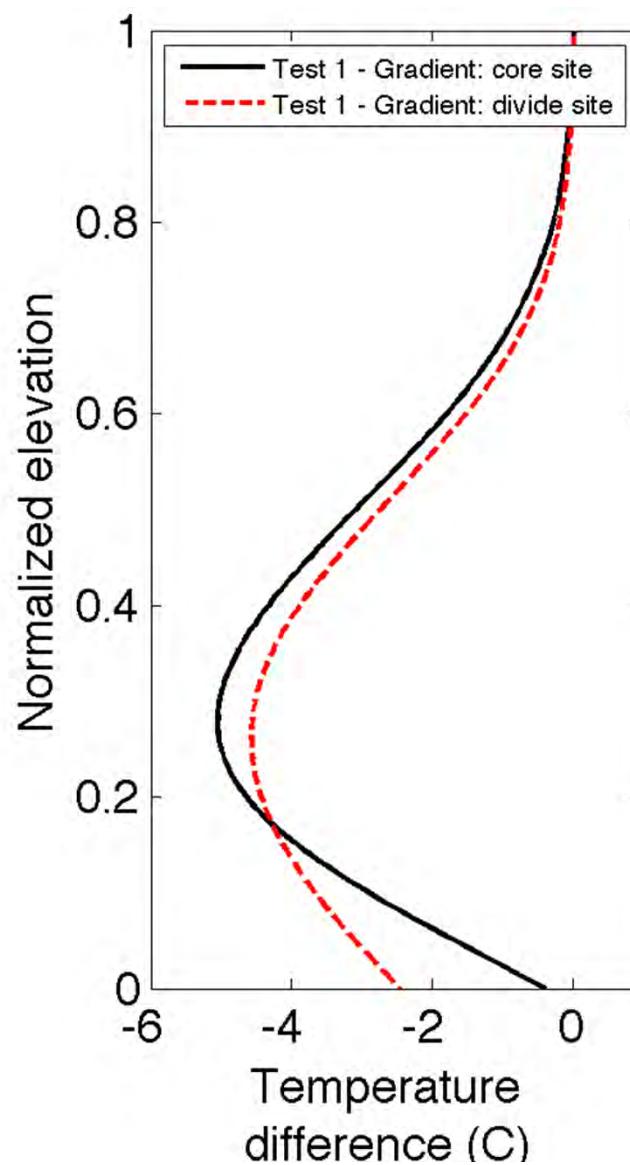
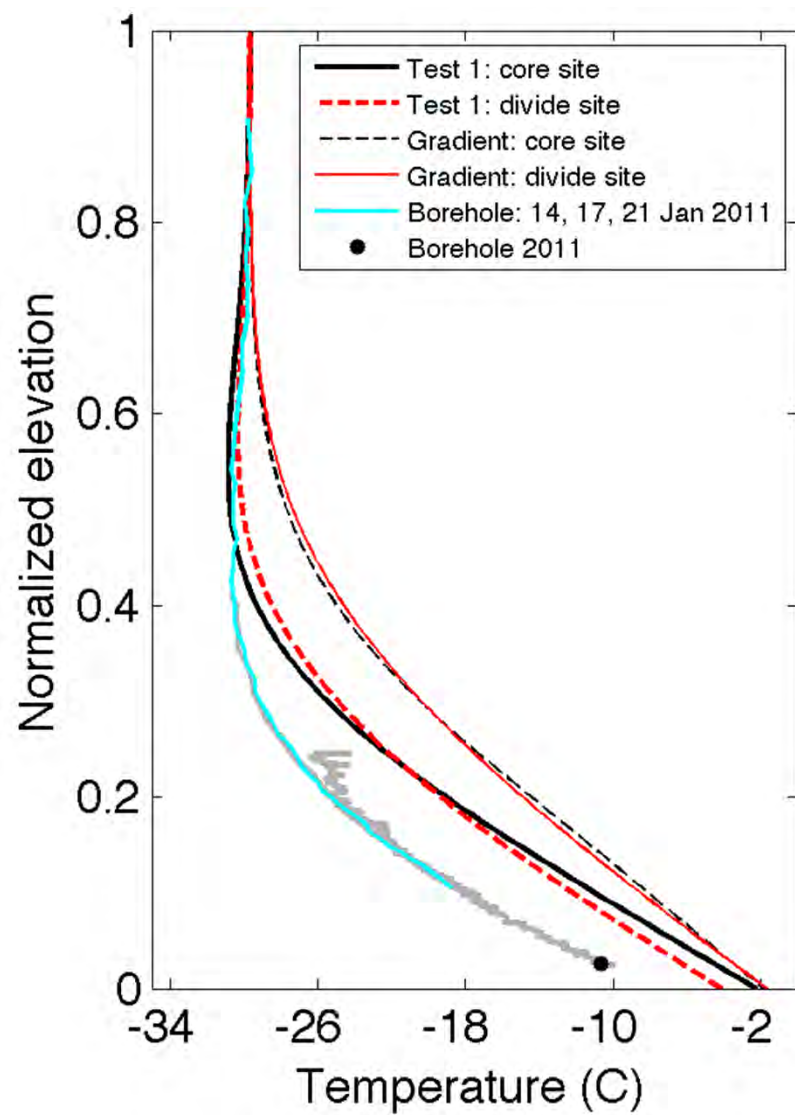


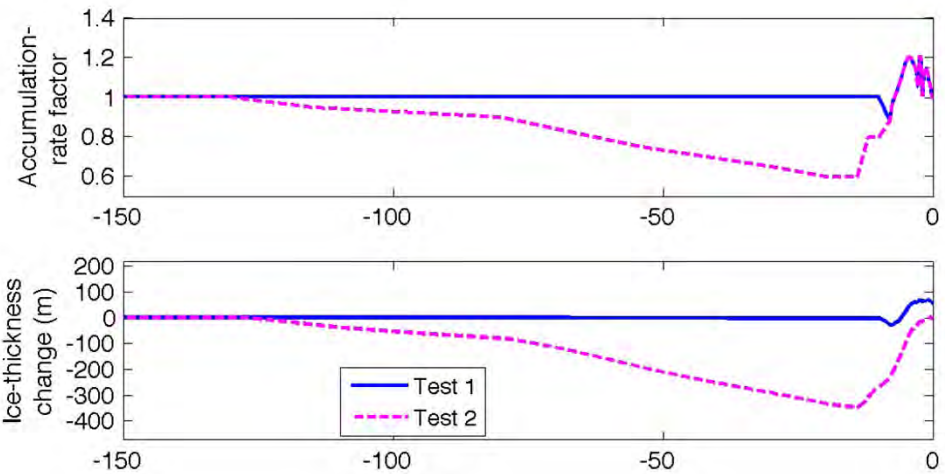
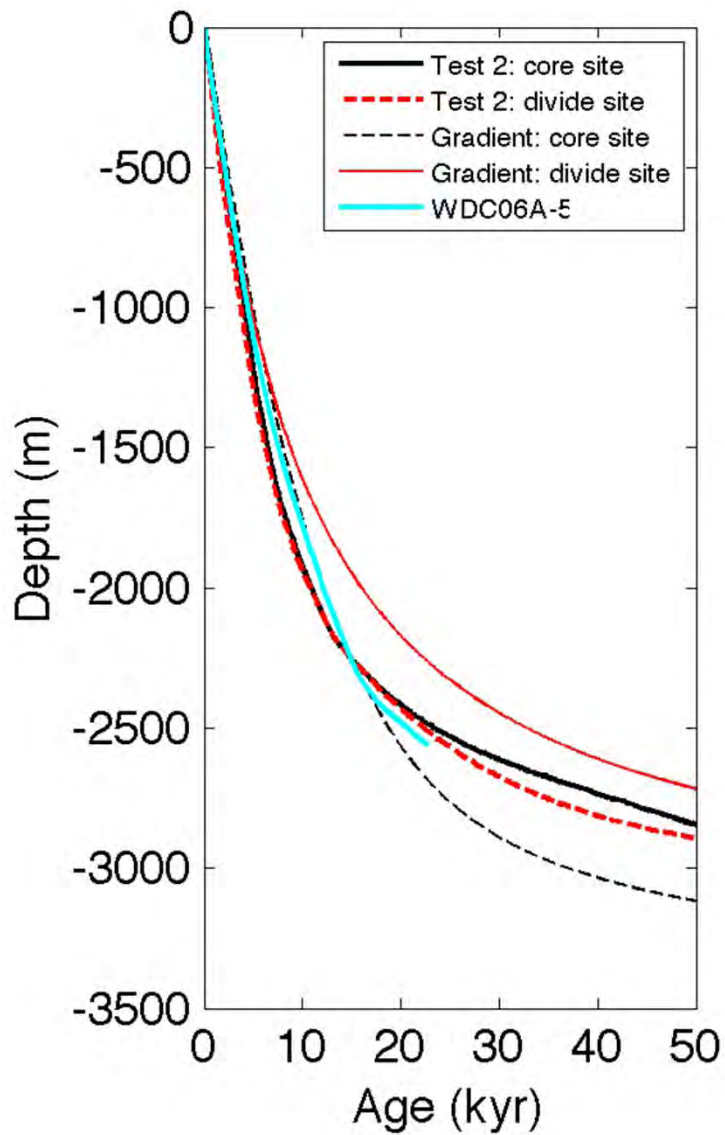
***Gradient in accumulation rate  
and Test 1  
at the core site vs. divide site***

*With accumulation rate constant in the glacial and increased in the Holocene, ice at the core site is deeper compared to constant accumulation*



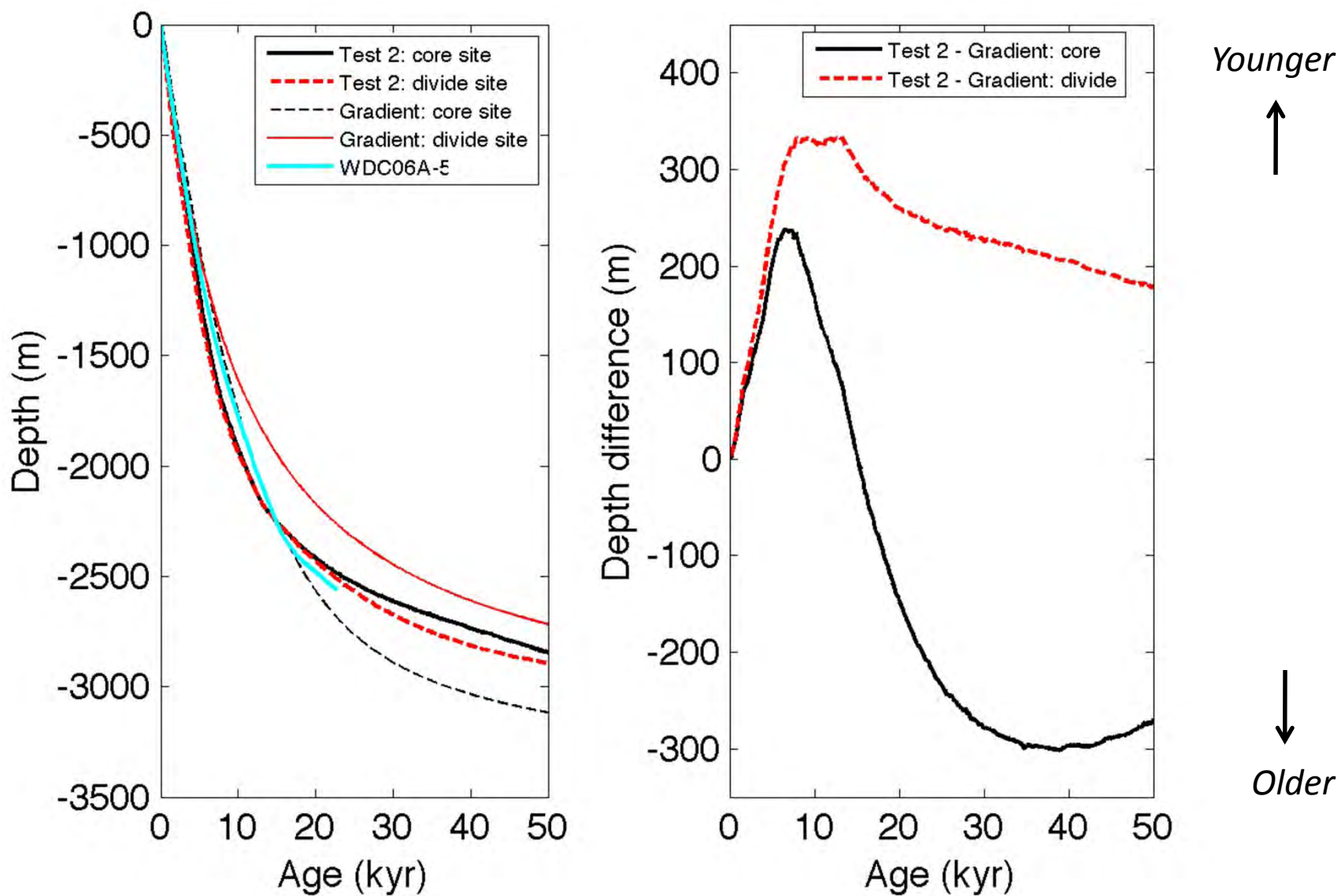
With ice-surface temperature variations, the **temperature profile** reflects glacial changes



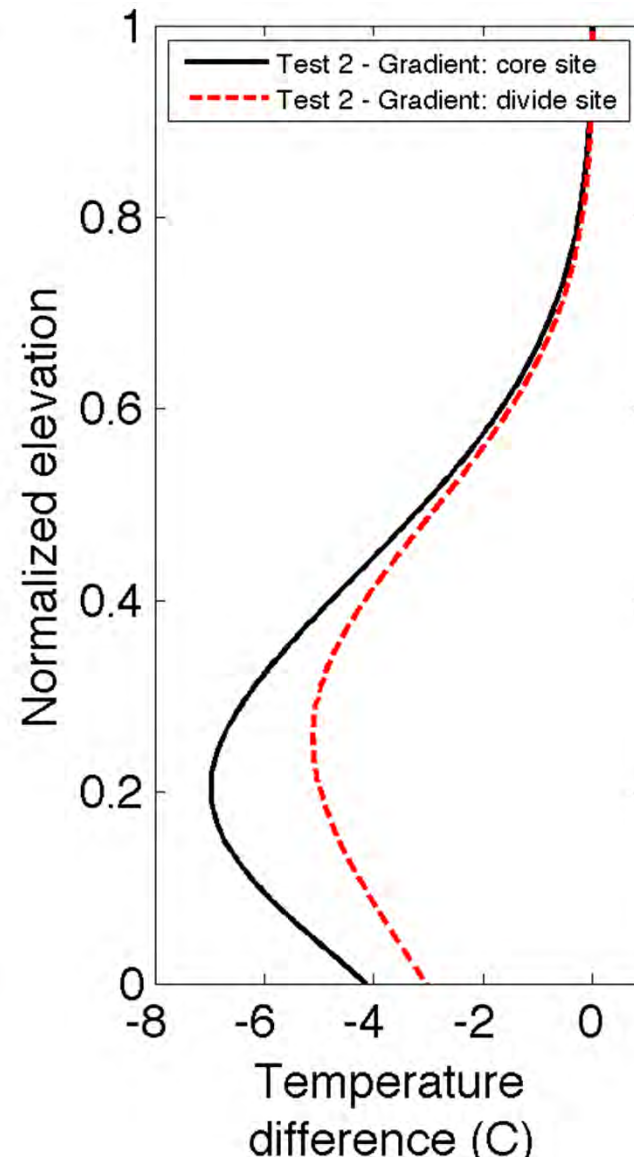
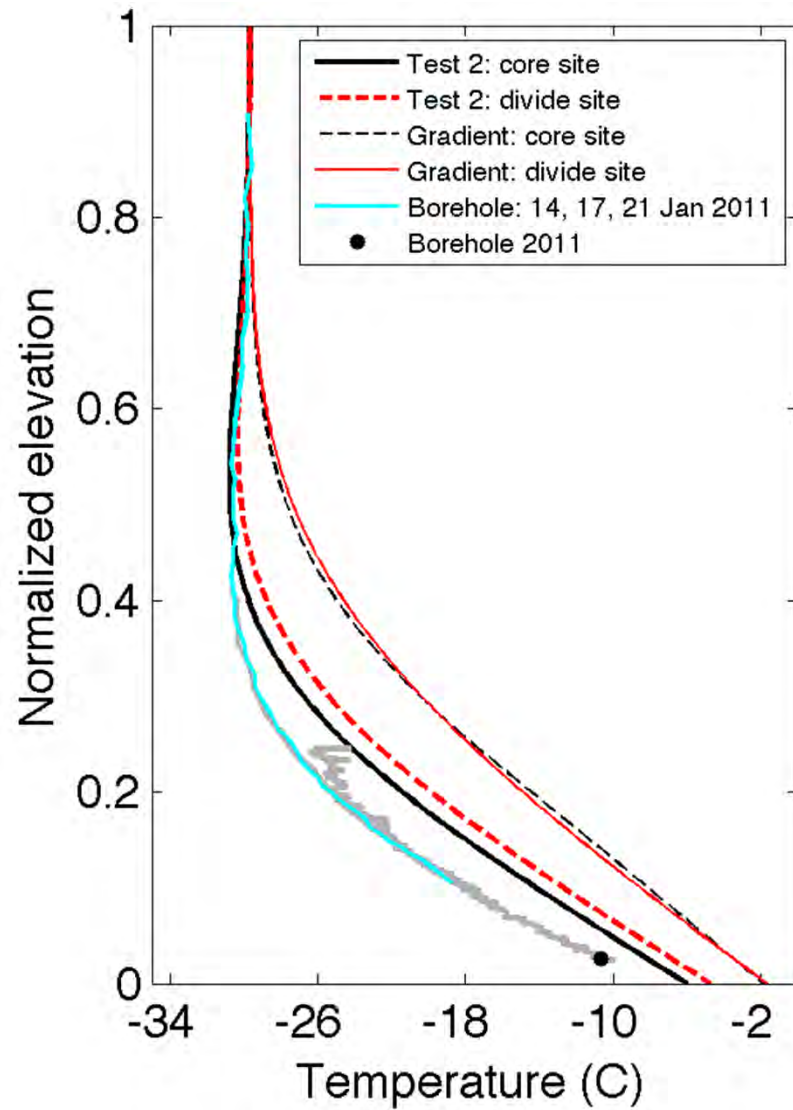


***Gradient in accumulation rate  
and Test 2  
at the core site vs. divide site***

*With accumulation rate decreased in the glacial and increased in the Holocene, the depth-age scales at the core site and at the divide site become similar*

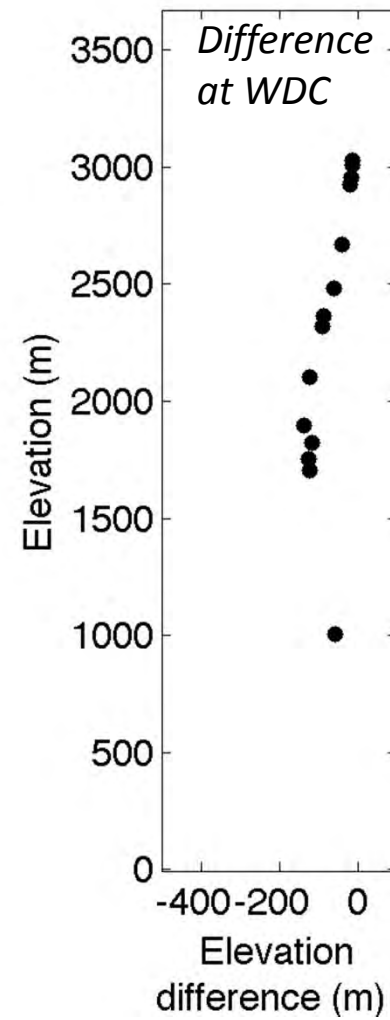
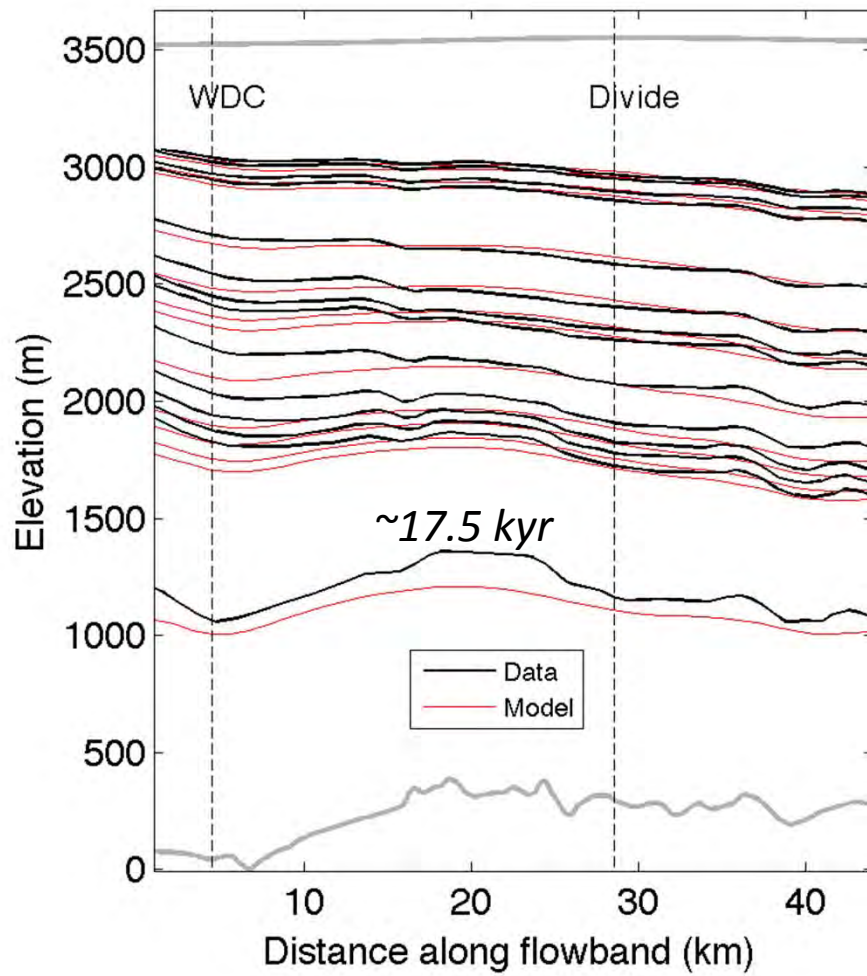
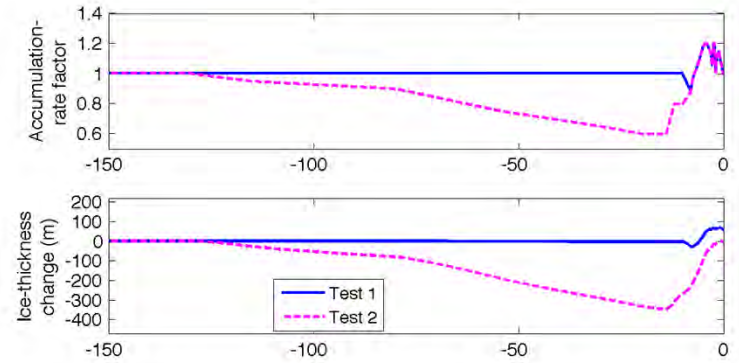


The **temperature profile** does not change significantly compared to test 1, but the core-site values are colder at depth

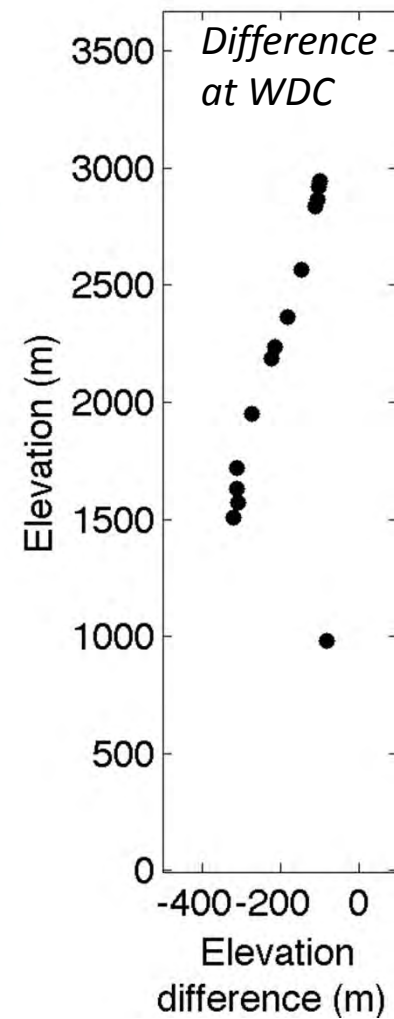
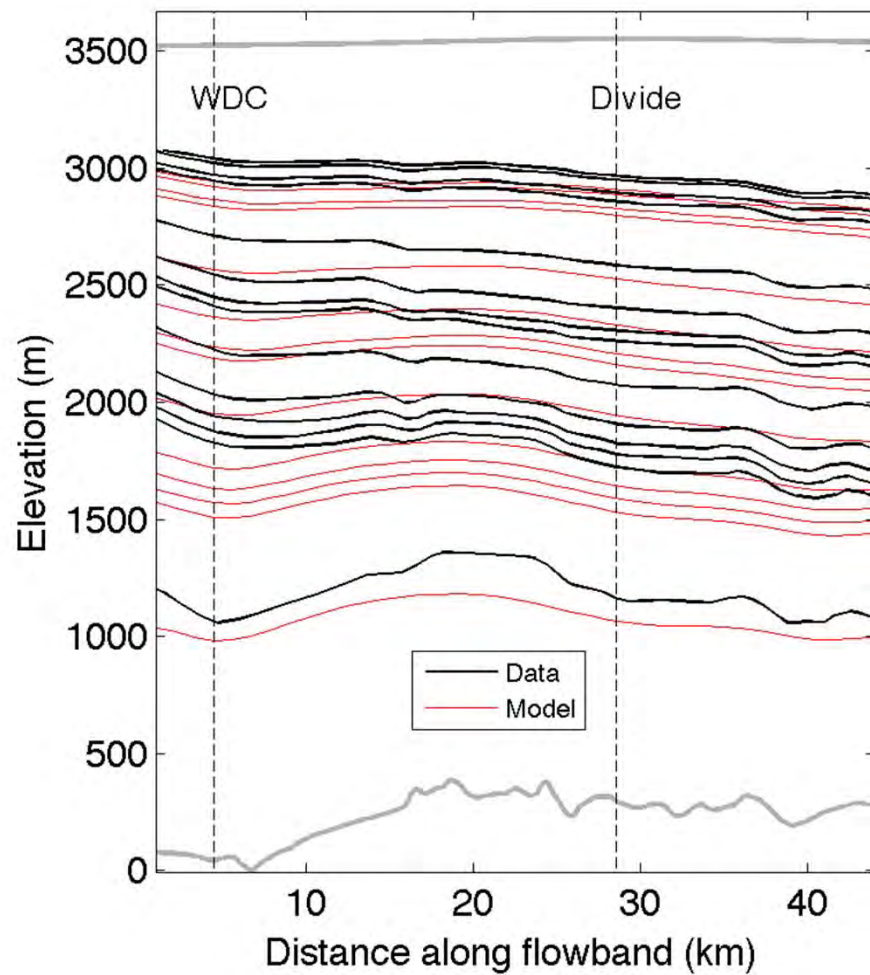
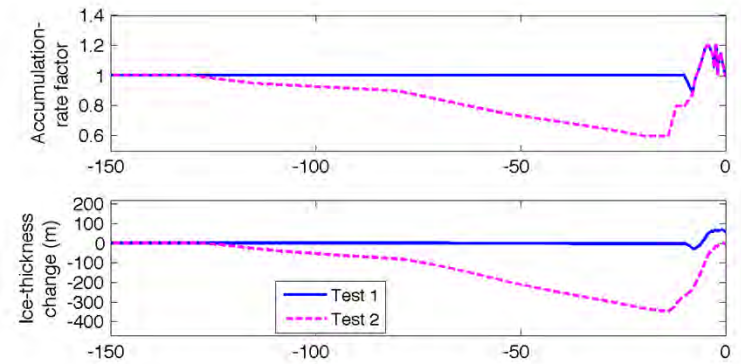




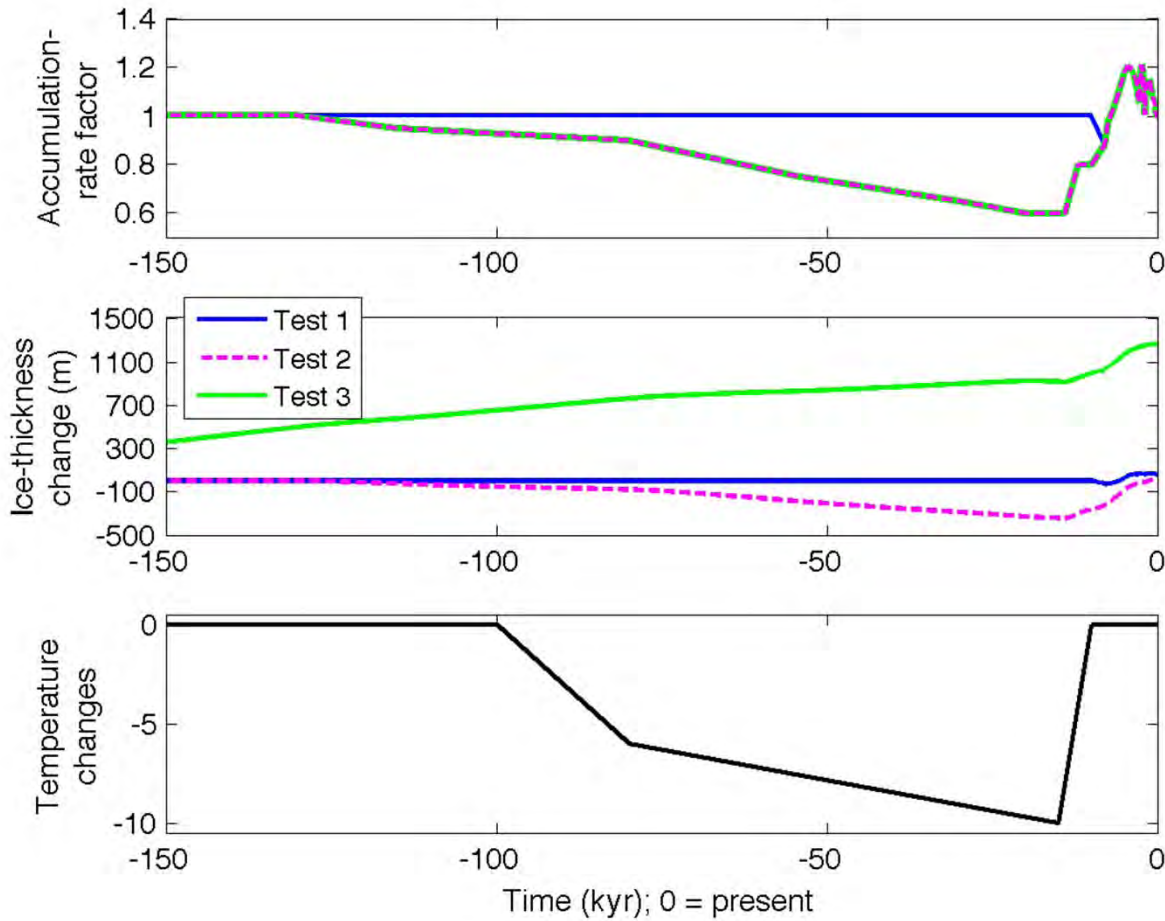
# Test 1: Internal layers



## Test 2: Internal layers



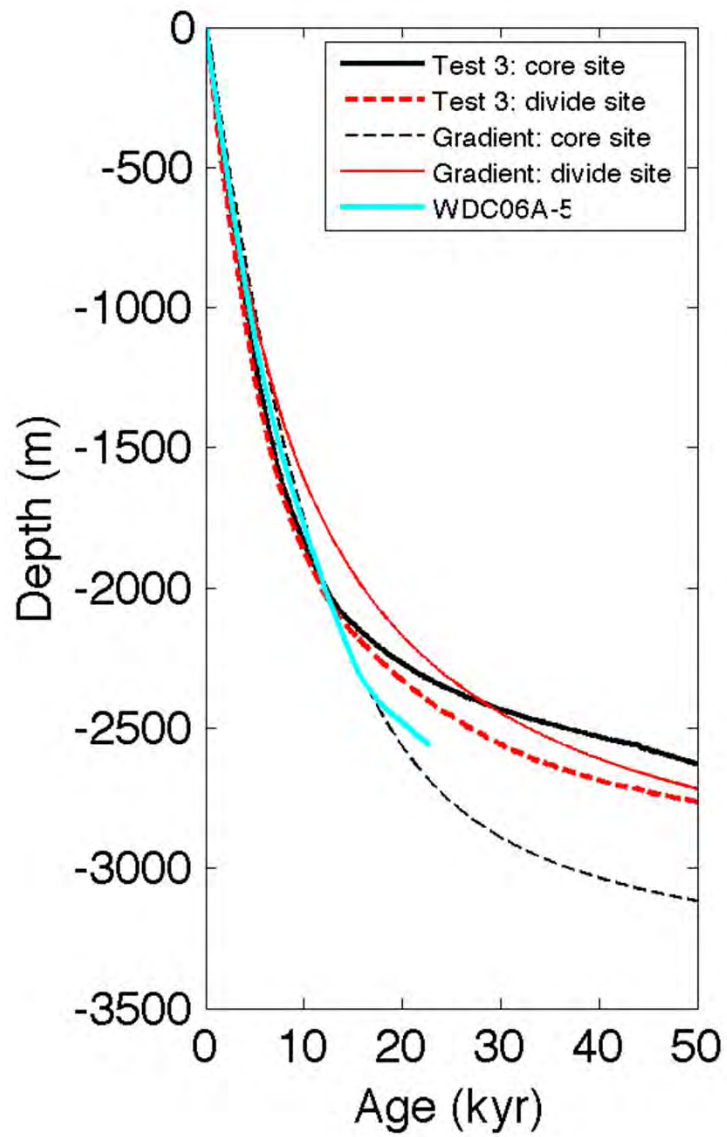
# Changes in ice flow



## Test 3:

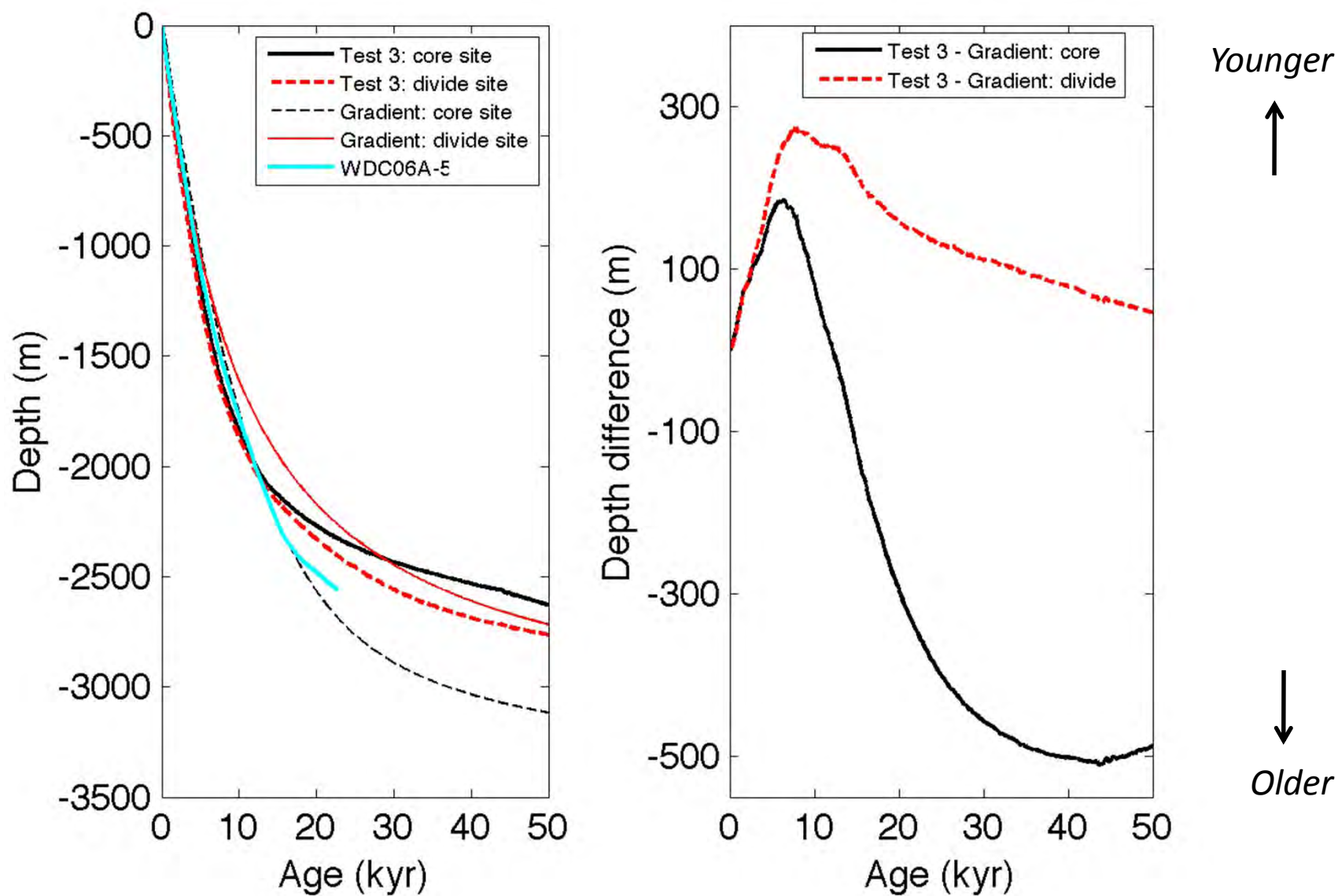
*Decreased accumulation in glacial  
Prescribed thickening (flow changes)  
Surface temperature changes*

*Thickening gives similar modern  
ice thickness as test 2*

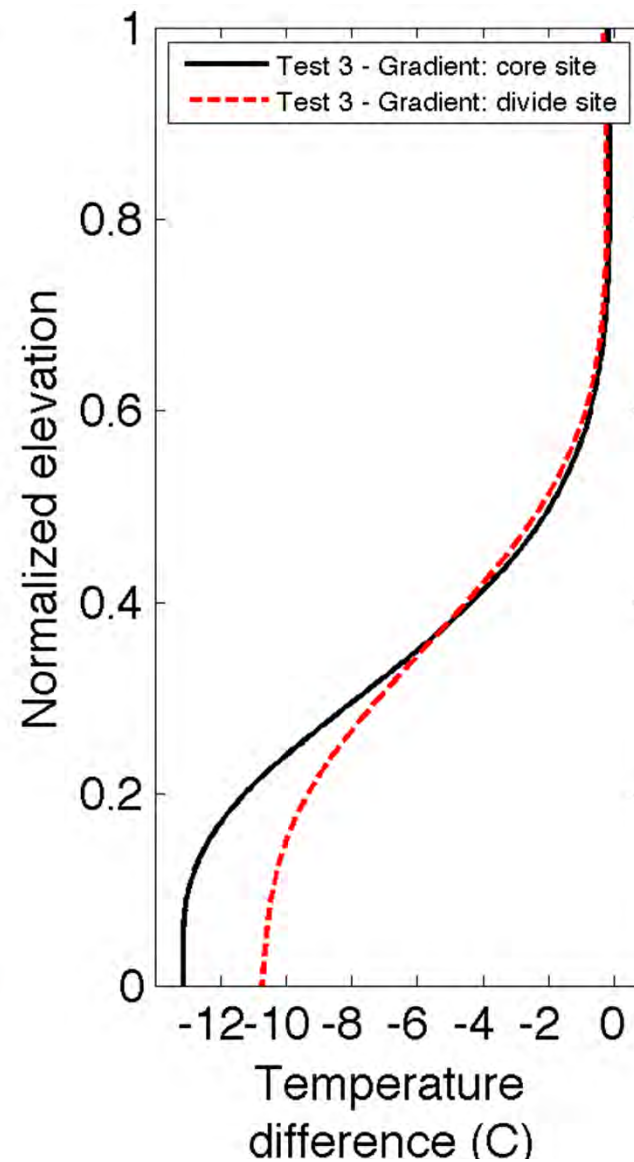
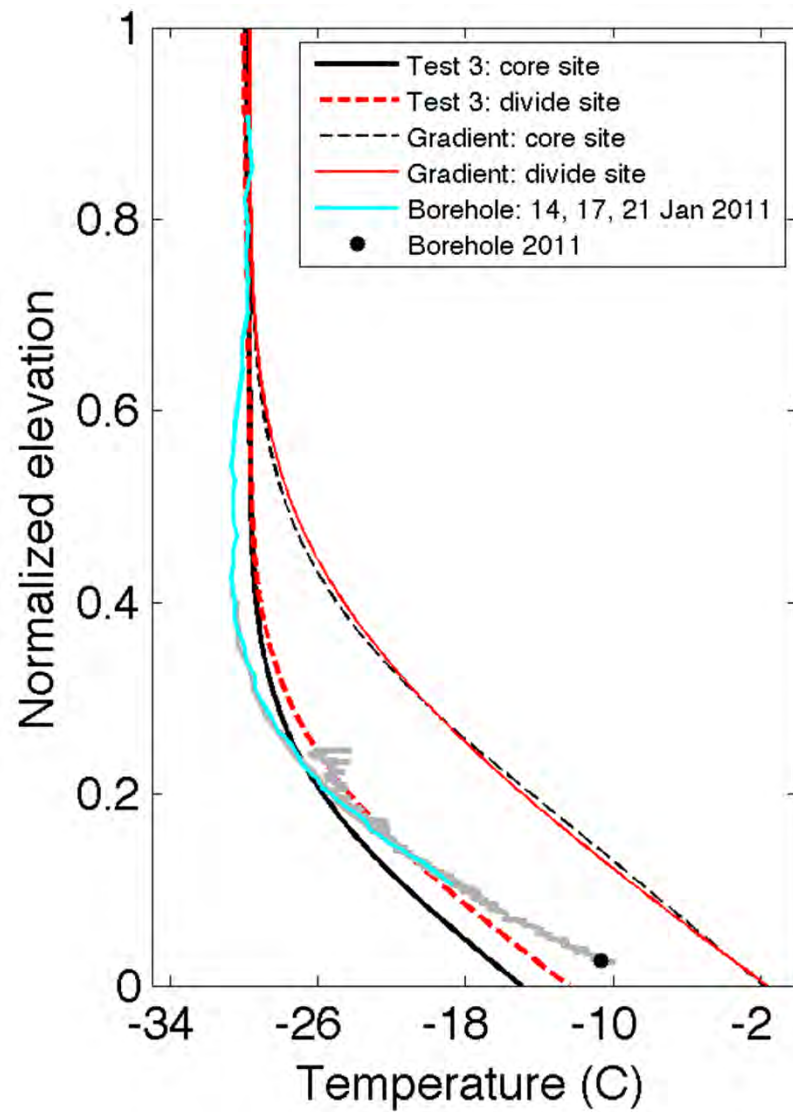


***Gradient in accumulation rate  
and Test 3  
at the core site vs. divide site***

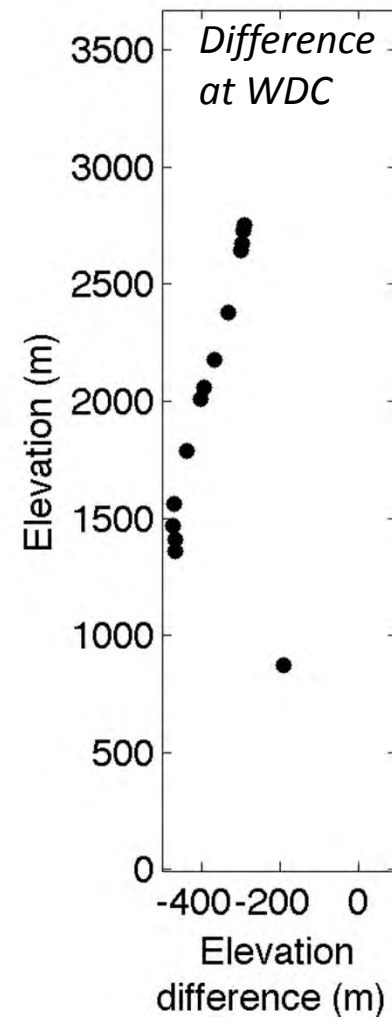
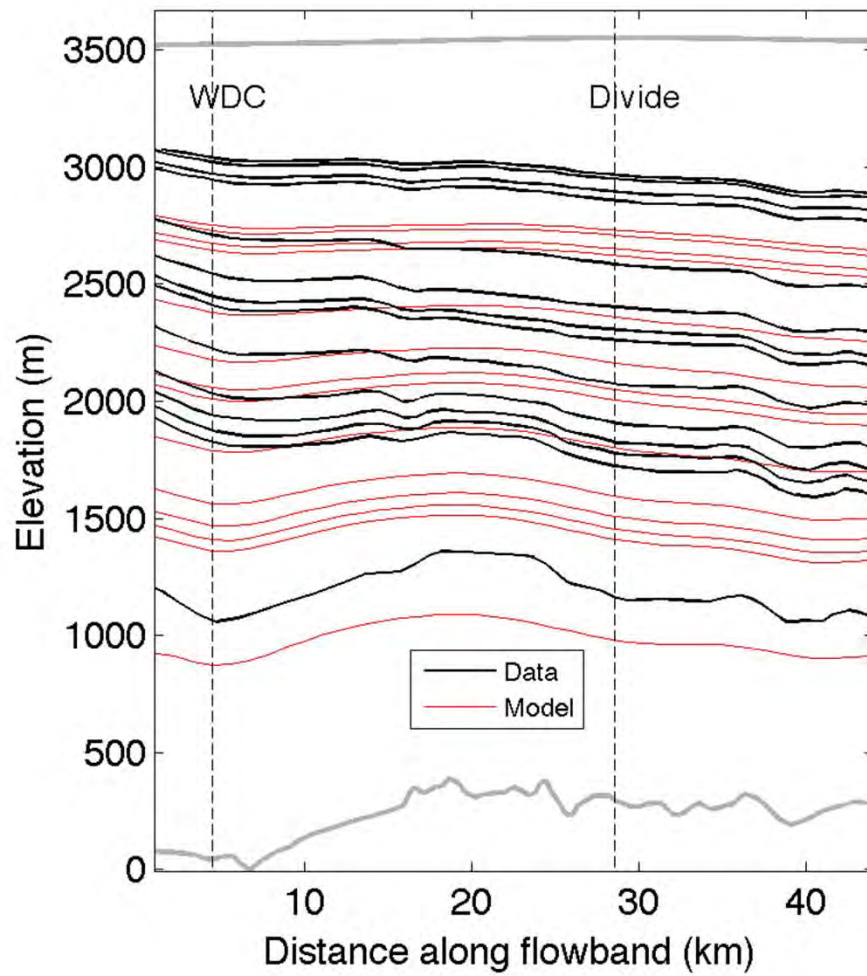
*With significant ice thickening the difference in the depth-age scales is similar to the case with the same accumulation-rate changes but with thinning in the glacial*



However, the **temperature profile** does change significantly compared to test 2, the ice-thickness changes are reflected in the ice temperature at depth



### Test 3: Internal layers



## Summary

Accumulation-rate changes can have a larger influence on the depth-age scale compared to ice-thickness changes

Ice-thickness changes can have a larger influence on the ice-temperature profile compared to accumulation-rate changes

The internal layers may provide context to separate the influence of changes in accumulation rate, ice thickness, and ice flow at the core site



# Objectives

## 1. Compare 2-D ice-sheet model realizations to ice-sheet data:

- Ice-core depth-age scale
- Ice-temperature profile
- Surface-velocity measurements
- Modern ice-surface profile
- Internal-layer shapes

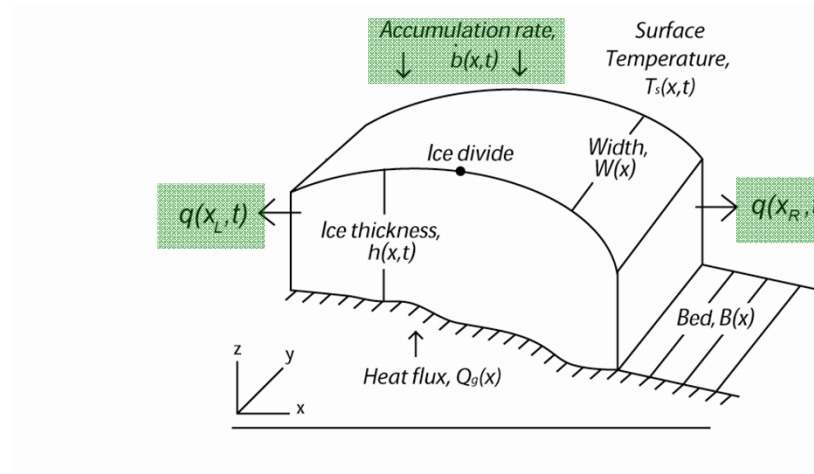
## 2. Solve an inverse problem to infer:

- Accumulation-rate history
- Ice-flow history (external-flux forcing) → ice-divide position

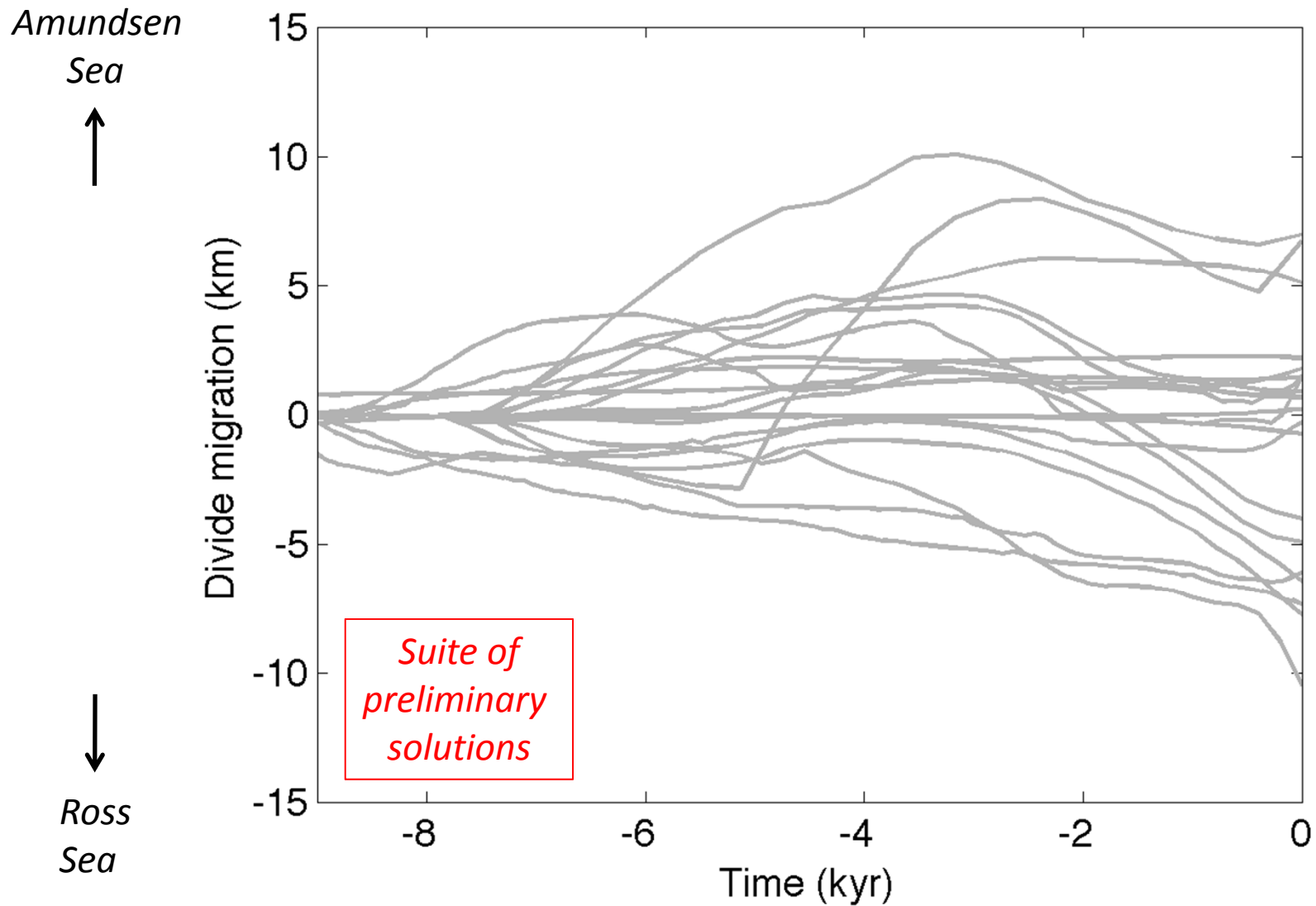
# How long has the WAIS divide been migrating?

Solve a *suite* of inverse problems for:

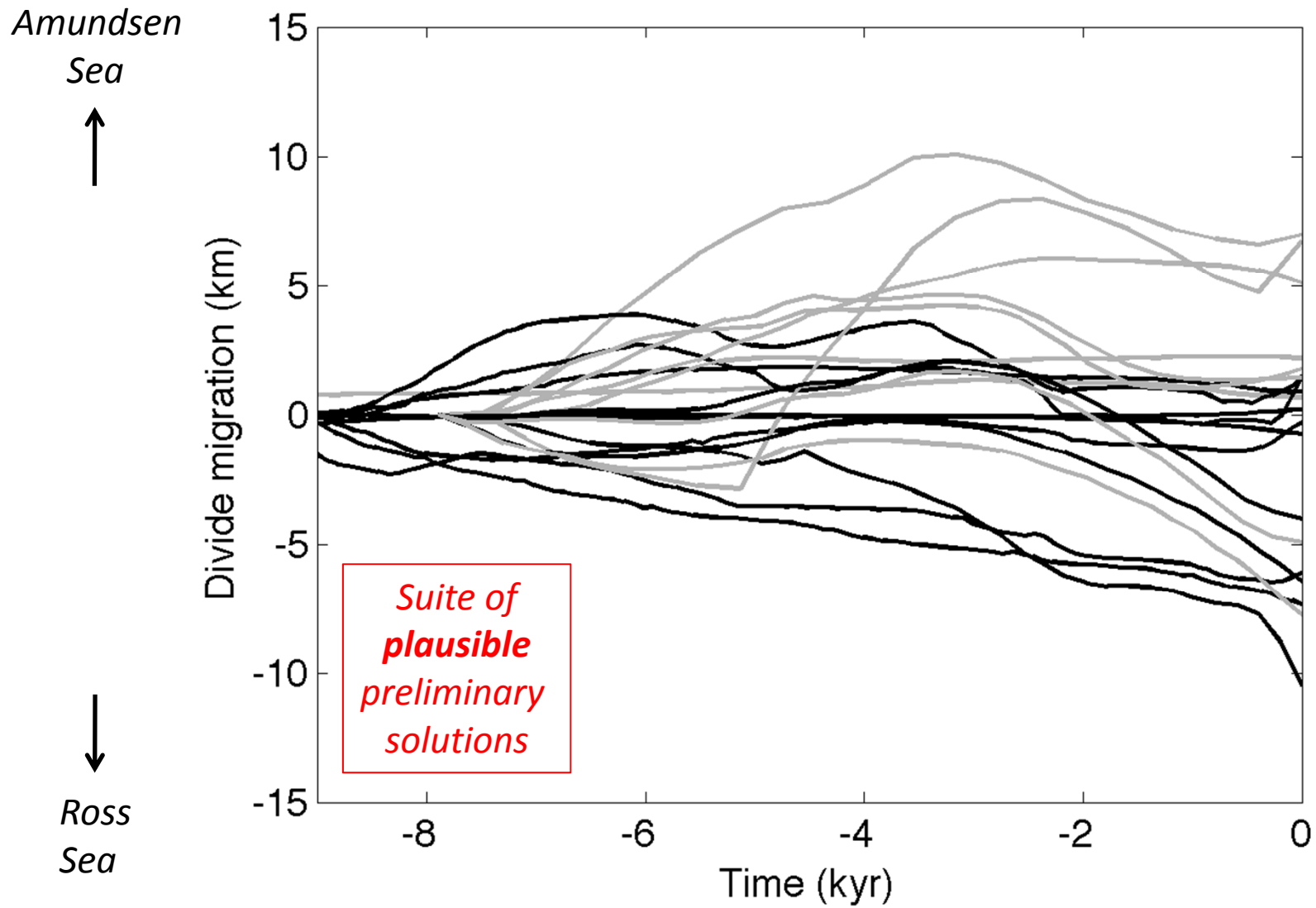
- only **accumulation-rate history**
- only **external-flux history**
- both **accumulation-rate and external-flux history**



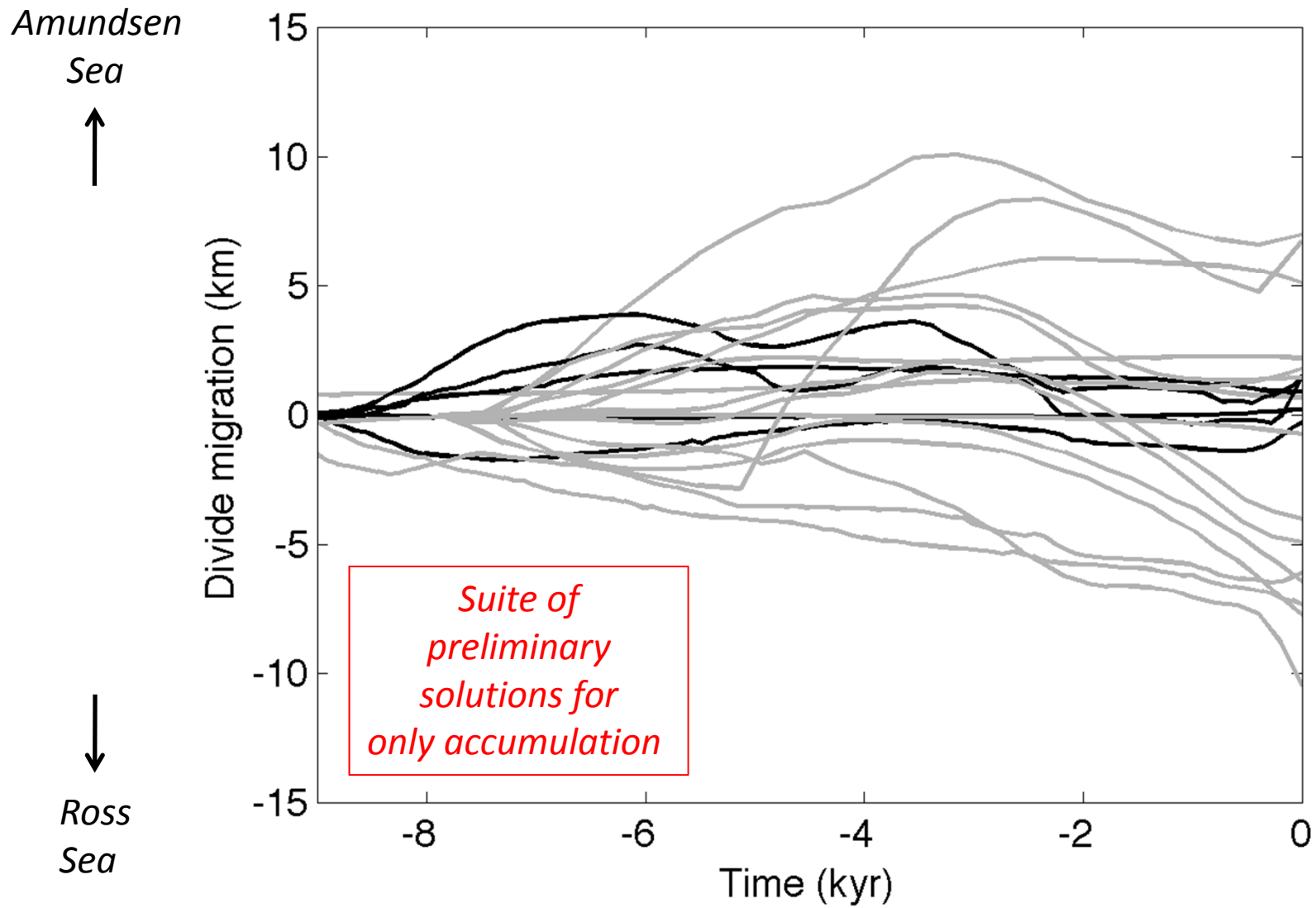
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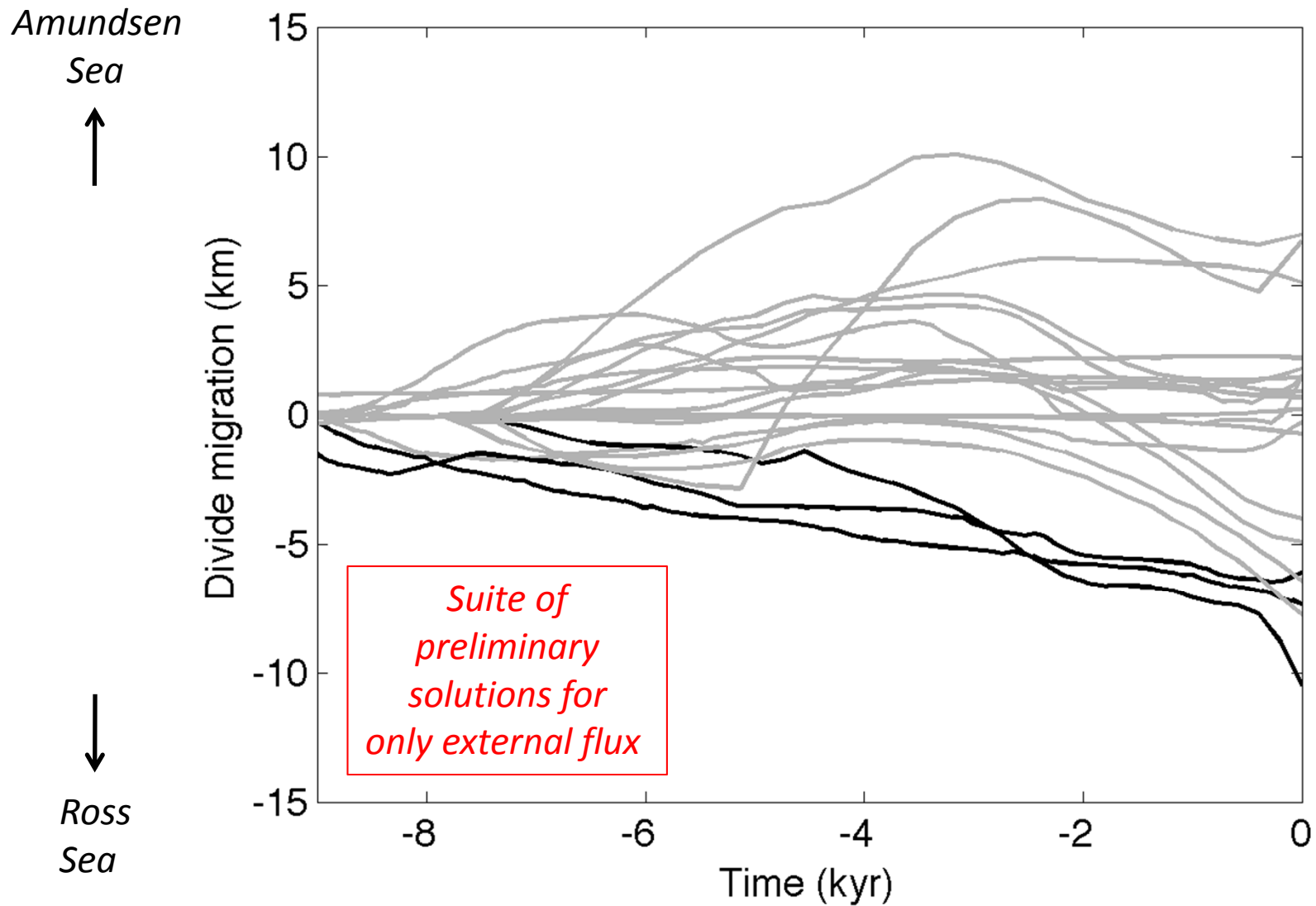
# How long has the WAIS divide been migrating?



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~~How long has the WAIS divide been migrating?~~

**How can we obtain the best set of possible solutions?**

**1.** Incorporate additional *data*:

- Ice-core depth-age scale
- Ice-temperature profile
- Internal layers

This is in  
progress

**2.** Incorporate additional *constraints*:

- Behavior characteristics of external-flux forcing
- Better guess at initial conditions

This needs  
input

~~How long has the WAIS divide been migrating?~~

**What can we say so far?**

Without changes in external flux over the past 9 kyr, unrealistic histories of accumulation are inferred to fit the data

Without changes in external flux over the past 9 kyr, the model cannot generate a good fit to the layers *and* to the modern ice-sheet data

Solving for a history over 9 kyr is likely sensitive to the initial conditions and this should be explored (e.g. solving problem further back in time)



## Summary / Conclusions

Accumulation-rate changes have a larger influence on the depth-age scale compared to ice-thickness changes

Ice-thickness changes have a larger influence on the ice-temperature profile compared to accumulation-rate changes

The internal layers, when used with depth-age and ice-temperature data, provide context to infer changes in accumulation rate, ice thickness, and ice flow at the core site – should consider 2-D effects

*All available data and constraints are necessary to use in the inverse problem to infer the history of WAIS Divide migration – layers provide the spatial information*



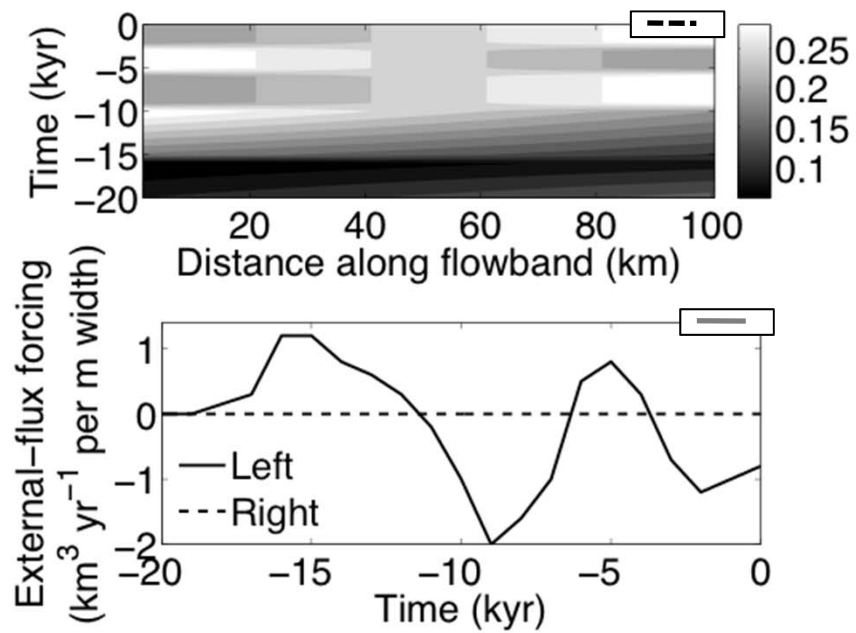
<b>Data value</b>	<b>Size</b>	<b>Symbol</b>
Internal-layer shapes	$N_{layers} \times N_h$	$h_d(x,z)$
Modern ice-surface topography	$N_S$	$S(x,t_0)$
Modern accumulation rate	$N_b$	$\dot{b}(x,t_0)$
Modern surface velocity	$N_u$	$u(x,t_0)$

<b>Model parameter</b>	<b>Size</b>	<b>Symbol</b>
Accumulation-rate history	$N_t \times N_x$	$\dot{b}(x,t)$
External-flux history	$N_t \times [ N_x^1 N_x^{end} ]$	$Q_{ext}(x,t)$
Ice flux entering the domain at initial timestep	1	$Q_0^{in}$
Ice thickness at first spatial node at initial timestep	1	$S_0^{in}$
Temperature-independent ice-softness parameter	1	$A_0$
Average geothermal flux	1	$Q_{geo}$

# Accumulation gradient and transients vs. flow transients

## *Example case*

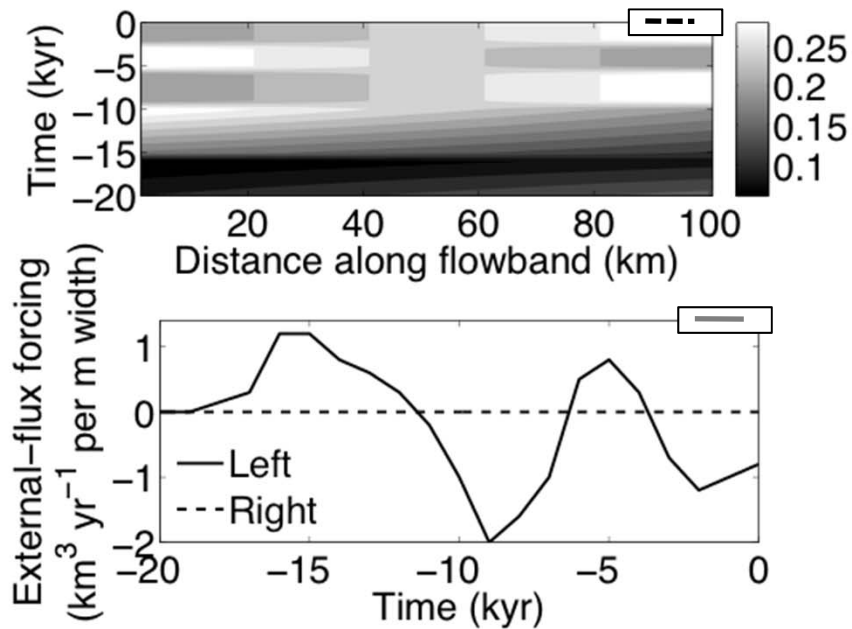
*Inputs: accumulation rate or external flux*



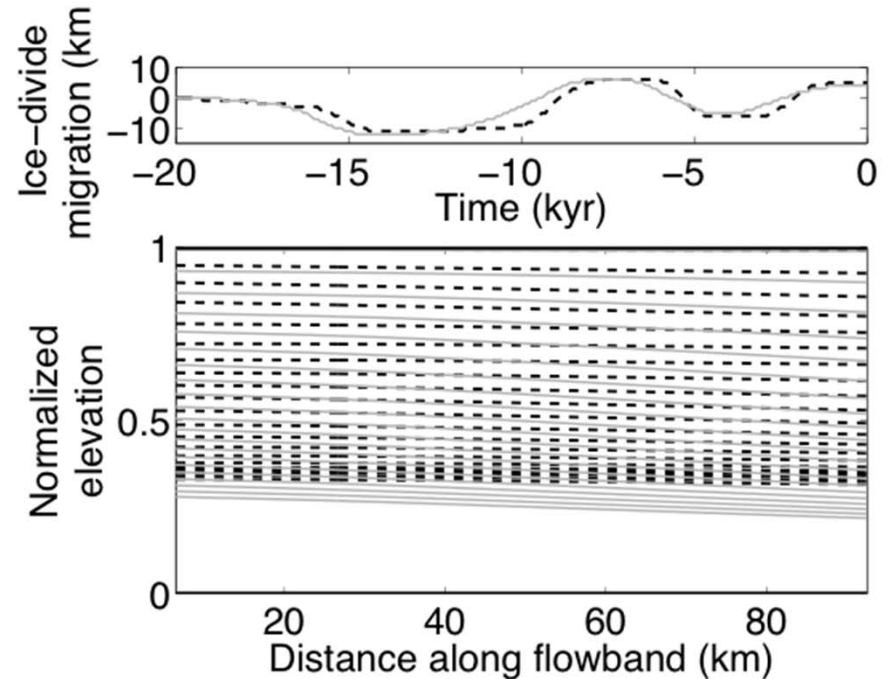
# Accumulation gradient and transients vs. flow transients

## Example case

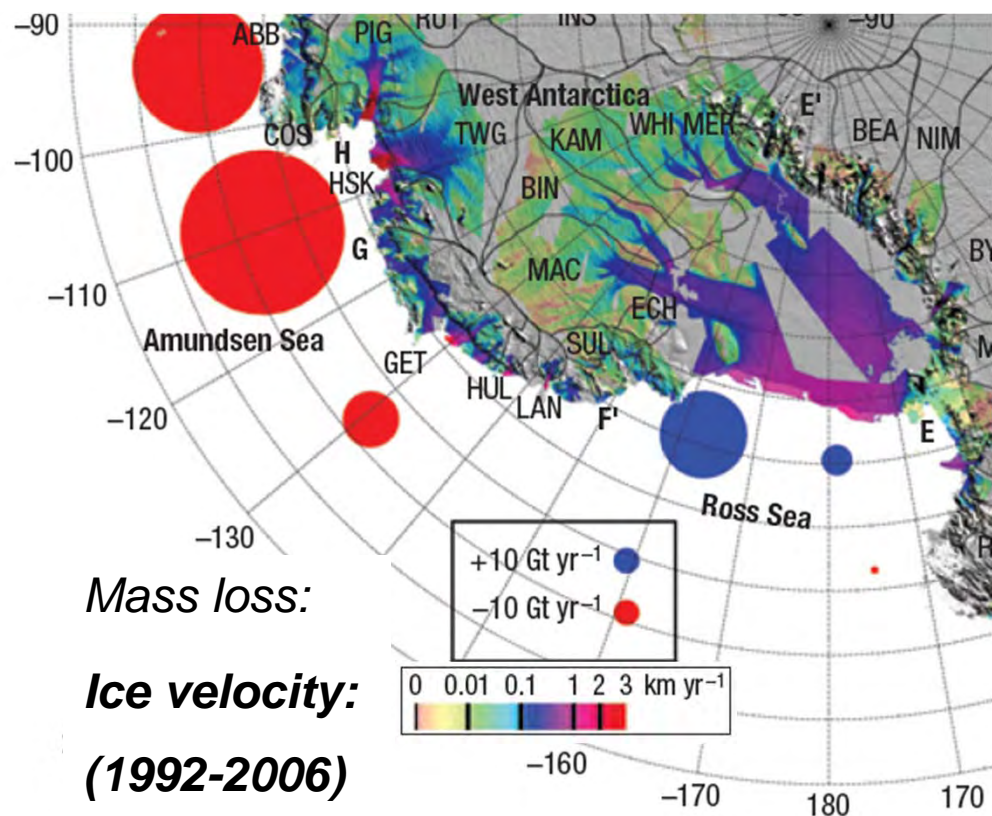
**Inputs:** accumulation rate or external flux



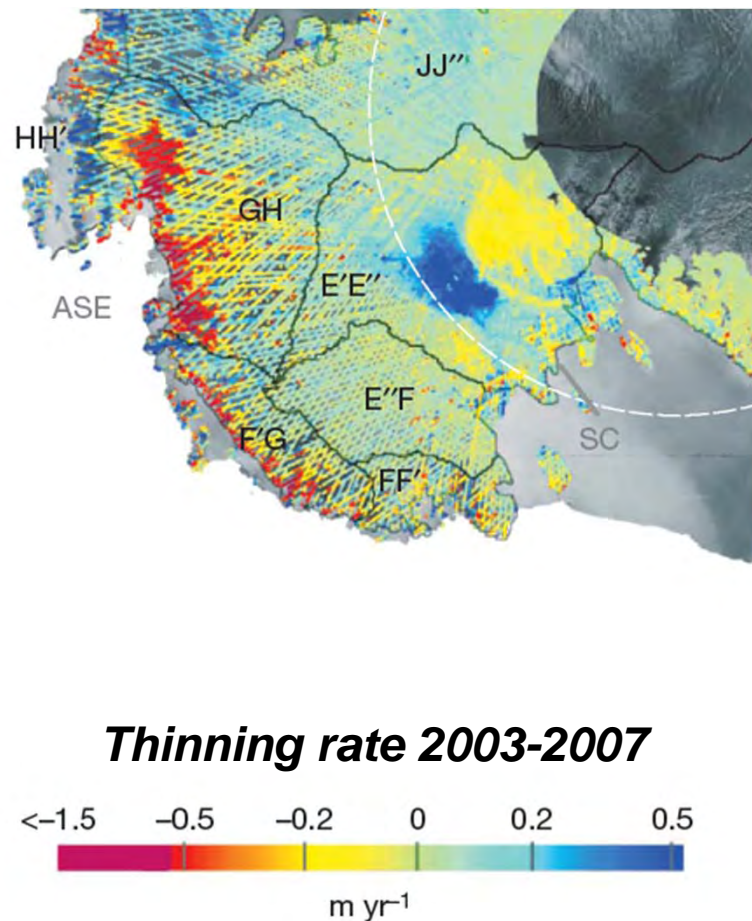
**Outputs:** ice-divide migration and internal-layer shapes



***Ice-divide position and interior ice thickness likely controlled by ice dynamics***



*Rignot et al. (2008)*  
*(Rignot et al. 2011)*



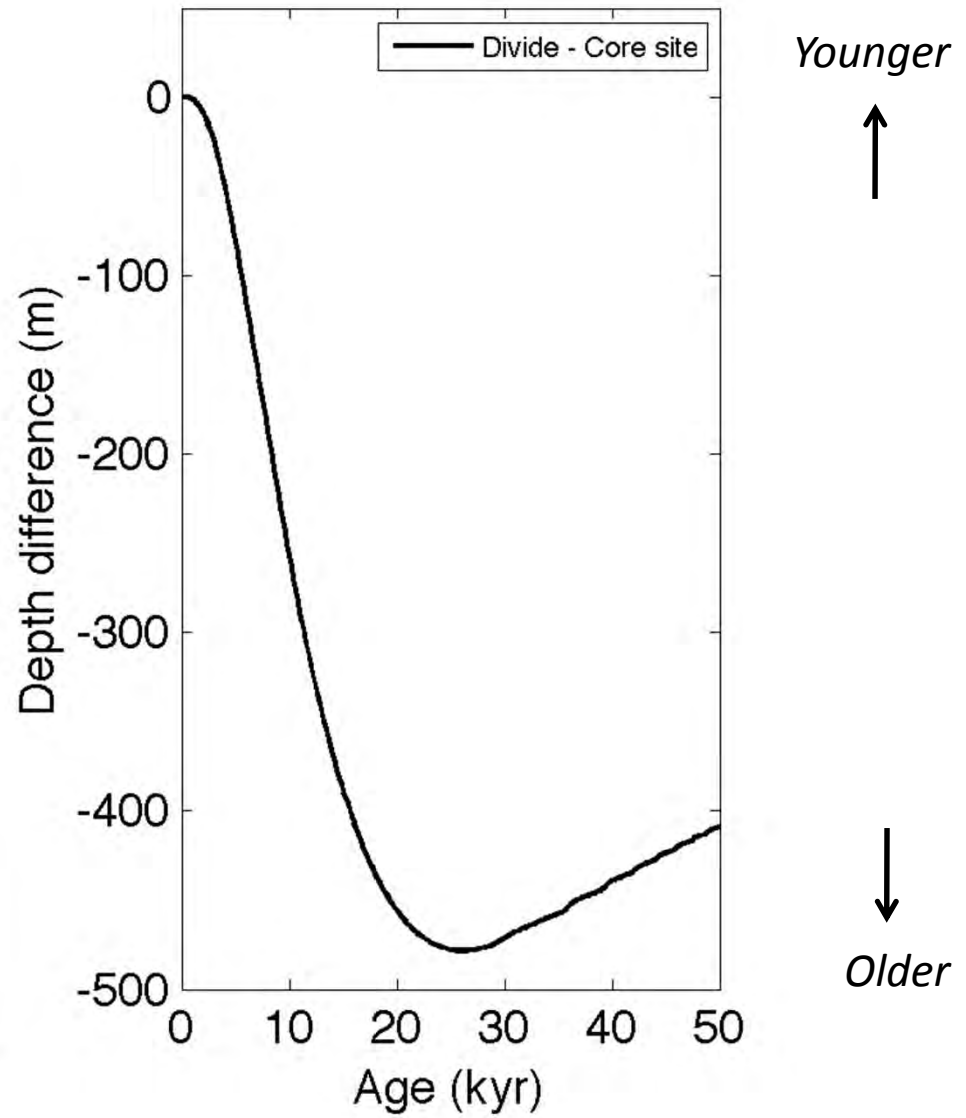
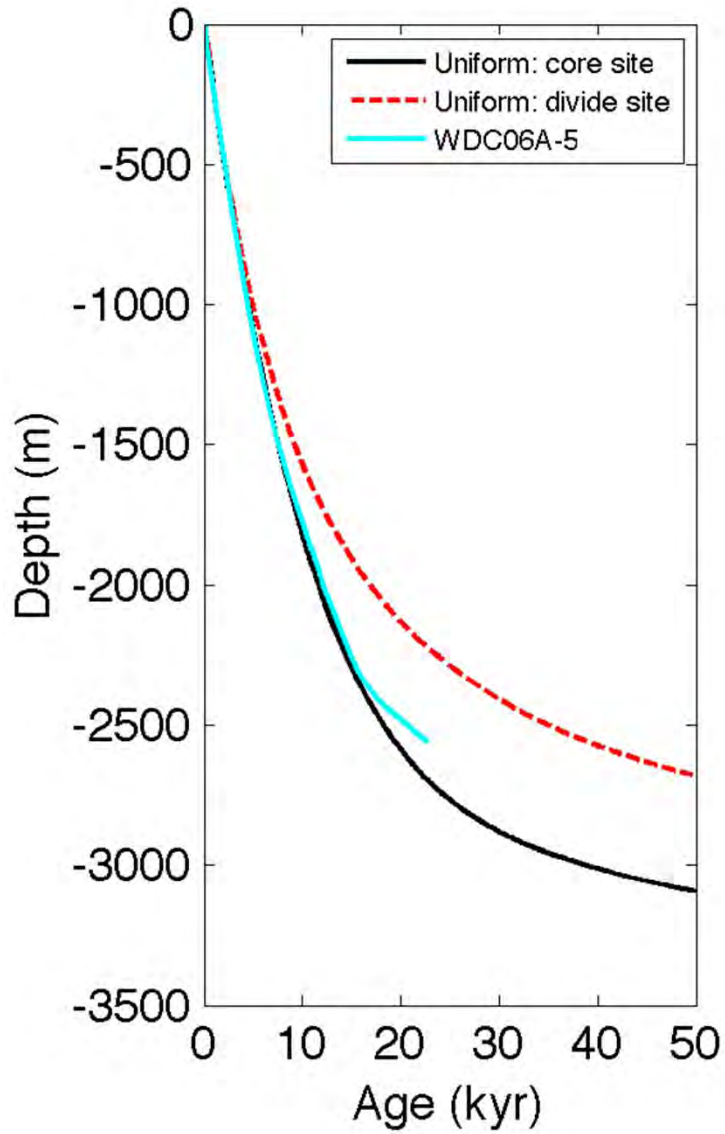
*Pritchard et al. (2009)*

Also e.g. Anadakrishnan et al. (1994), Marshall and Cuffey (2000), Gillet-Chaulet and Hindmarsh (2011)

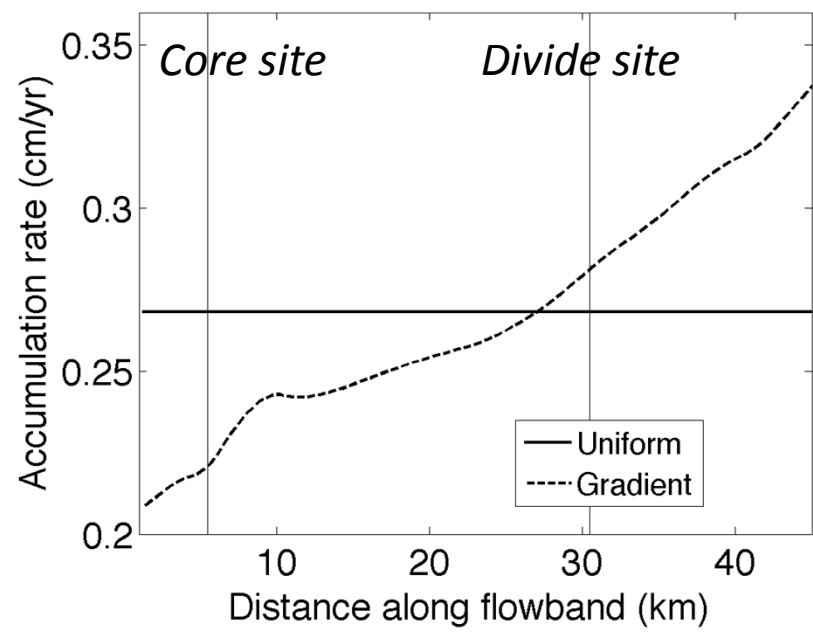
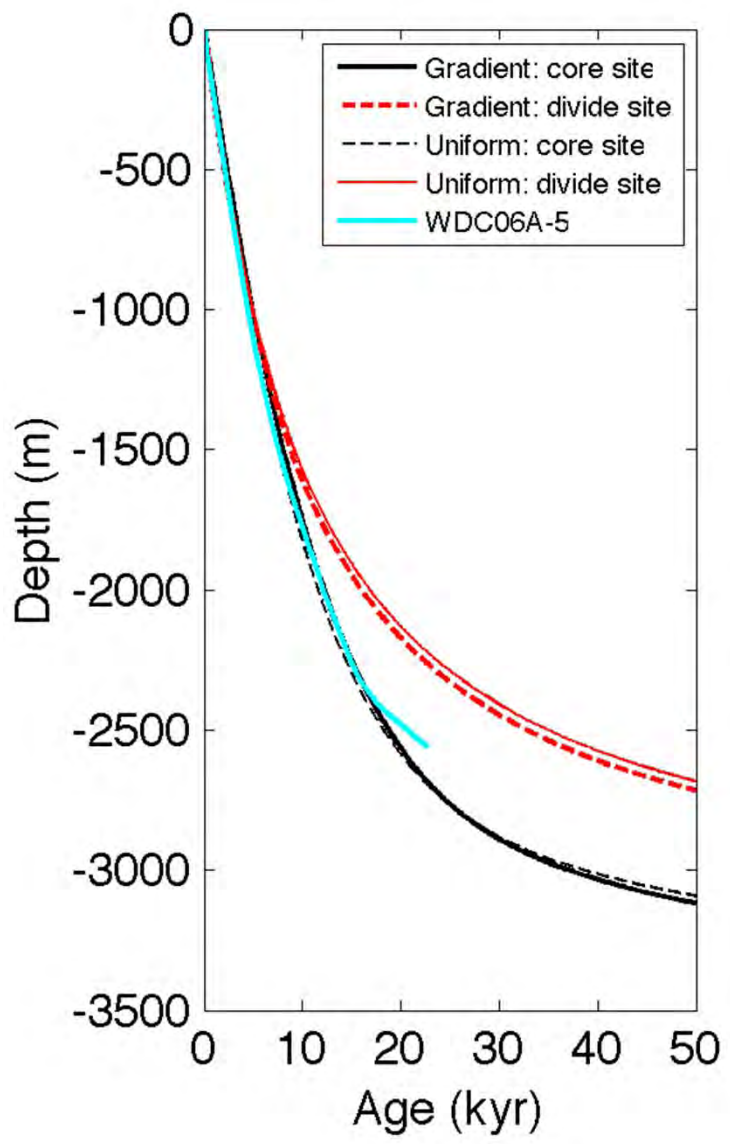
## The ice divide may migrate due to:

- Variations in the accumulation *pattern*
  - Transients in accumulation *rate*
  - Transients in ice flow (external-flux forcing)
- 
- \* prescribed surface-temperature history
  - \* prescribed heat flux
  - \* prescribed ice softness
  - \* no basal melting

With a uniform accumulation rate, ice at the core site is deeper compared to the divide







*Ice at the divide is consistently deeper because the accumulation rate is higher*

*Ice at the core site is shallower until ice is older than ~30 kyr because accumulation is lower*

